

updates on chemical evolution models

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Modeling chemical evolution

Valiante, Schneider, Salvadori & Bianchi, in prep

$$\begin{aligned} \frac{dM_*(t)}{dt} &= \text{SFR}(t) - \frac{dR(t)}{dt} \\ \frac{dM_{\text{ISM}}(t)}{dt} &= -\text{SFR}(t) + \frac{dR(t)}{dt} + \frac{dM_{\text{inf}}}{dt} - \frac{dM_{\text{ej}}}{dt} \\ \frac{dM_Z(t)}{dt} &= -Z_{\text{ISM}}(t)\text{SFR}(t) + \frac{dY_Z(t)}{dt} - Z_{\text{ISM}}(t) \frac{dM_{\text{ej}}}{dt} \\ \frac{dM_d(t)}{dt} &= -Z_d(t)\text{SFR}(t) + \frac{dY_d(t)}{dt} - \frac{M_d(t)}{\tau_d} - Z_d(t) \frac{dM_{\text{ej}}}{dt} \\ \frac{dM_{\text{inf}}}{dt} &= A \left(\frac{t}{t_{\text{inf}}} \right)^2 \exp \left(-\frac{t}{t_{\text{inf}}} \right). \end{aligned}$$

$$\begin{aligned} t_{\text{inf}} &= t_{\text{ff}}/4 \\ A &= M_{\text{gas,in}}/2 t_{\text{inf}} \end{aligned}$$

Keres et al. (2005); Salvadori et al. (2009)

$$\begin{aligned} \frac{dR(t)}{dt} &= \int_{m_*(t)}^{100M_\odot} (m - \omega_m(m, Z_{\text{ISM}})) \phi(m) \text{SFR}(t - \tau_m) dm \\ \frac{dY_Z(t)}{dt} &= \int_{m_*(t)}^{100M_\odot} m_Z(m, Z_{\text{ISM}}) \phi(m) \text{SFR}(t - \tau_m) dm \\ \frac{dY_d(t)}{dt} &= \int_{m_*(t)}^{100M_\odot} m_d(m, Z_{\text{ISM}}) \phi(m) \text{SFR}(t - \tau_m) dm \end{aligned}$$

Mechanical feedback

Mass ejection rate:

$$\frac{dM_{ej}}{dt} = \frac{2\epsilon_w \langle E_{SN} \rangle}{v_e^2} \frac{dN_{SN}}{dt}$$

kinetic energy by SN-driven winds

$$E_{SN} = \epsilon_w N_{SN} \langle E_{SN} \rangle$$

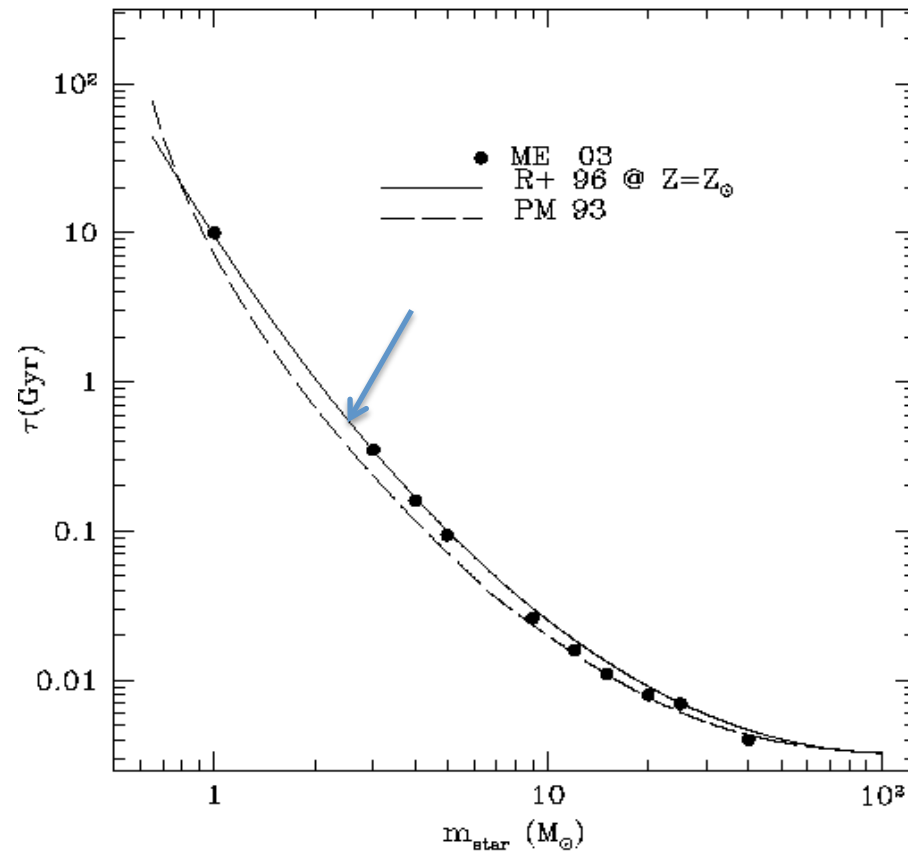
conversion efficiency: 0.002

10^{51} erg

escape velocity

$$v_e^2 = GM/r$$

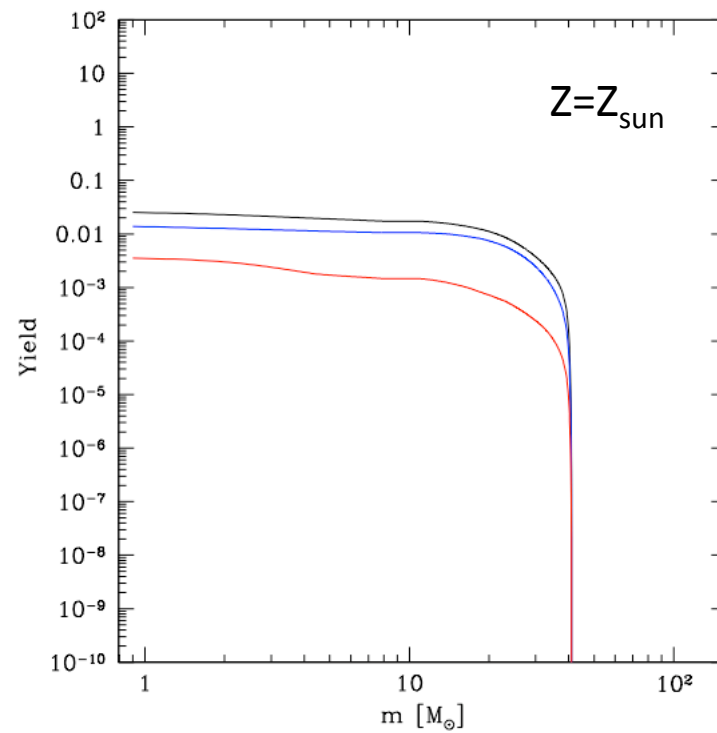
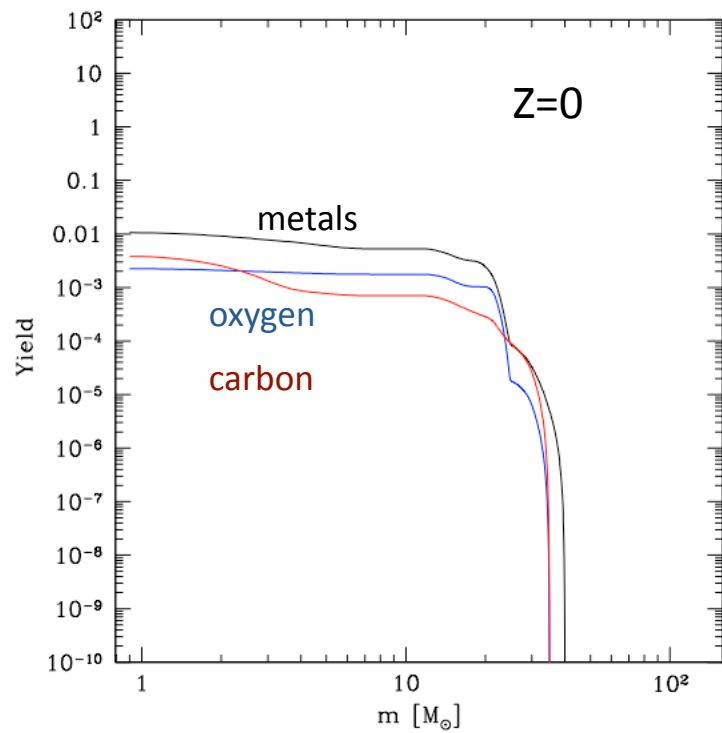
stellar lifetimes and IMF



$$\Phi(m) = \frac{dN}{dm} \propto m^{-1+x} \exp(-m_{\text{cut}}/m), \quad (2)$$

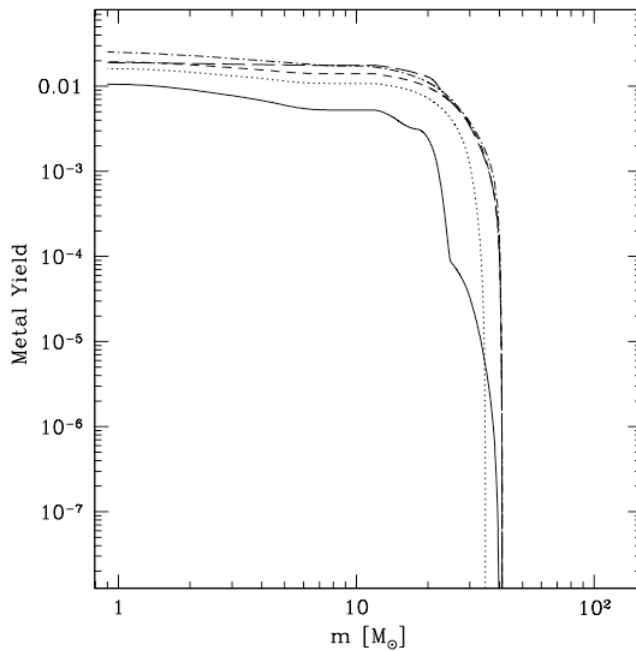
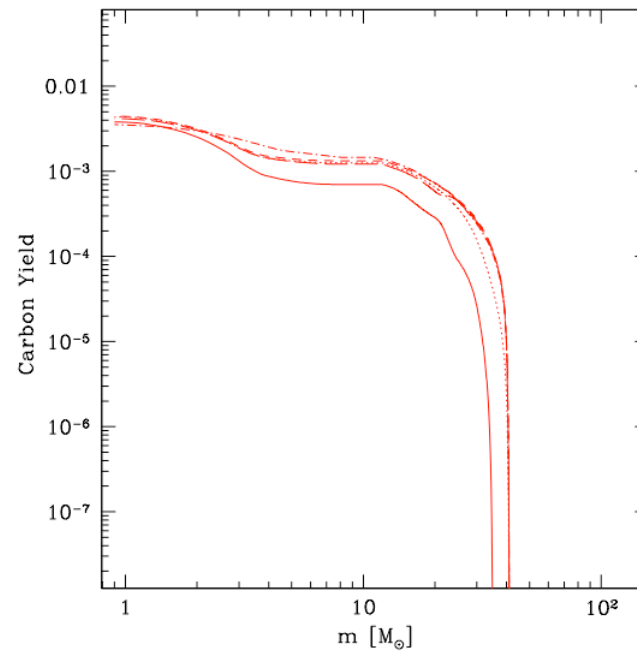
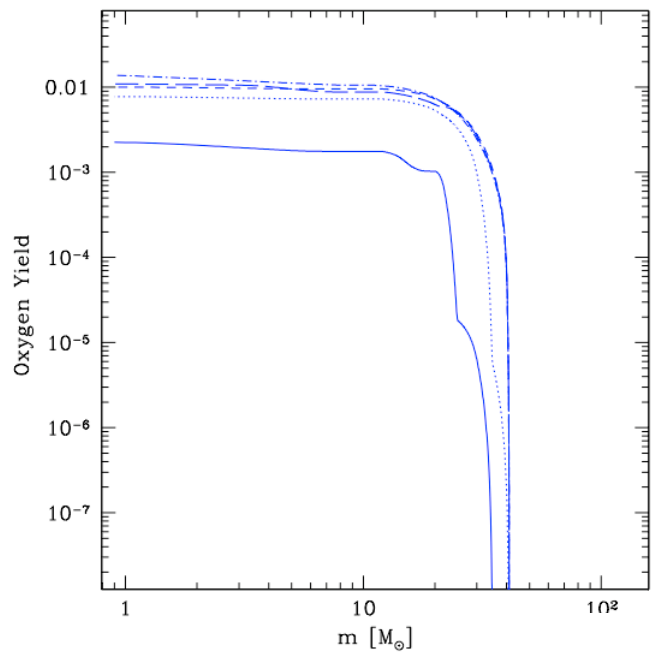
with $x = -1.35$, $m_{\text{cut}} = 0.35 M_{\odot}$ and m in the range $[0.1-100] M_{\odot}$

metal yields

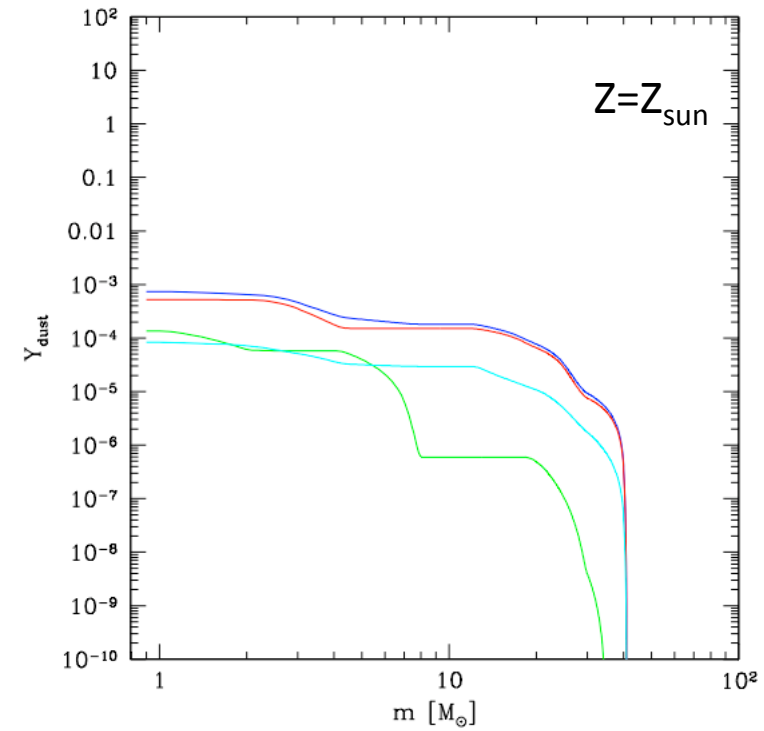
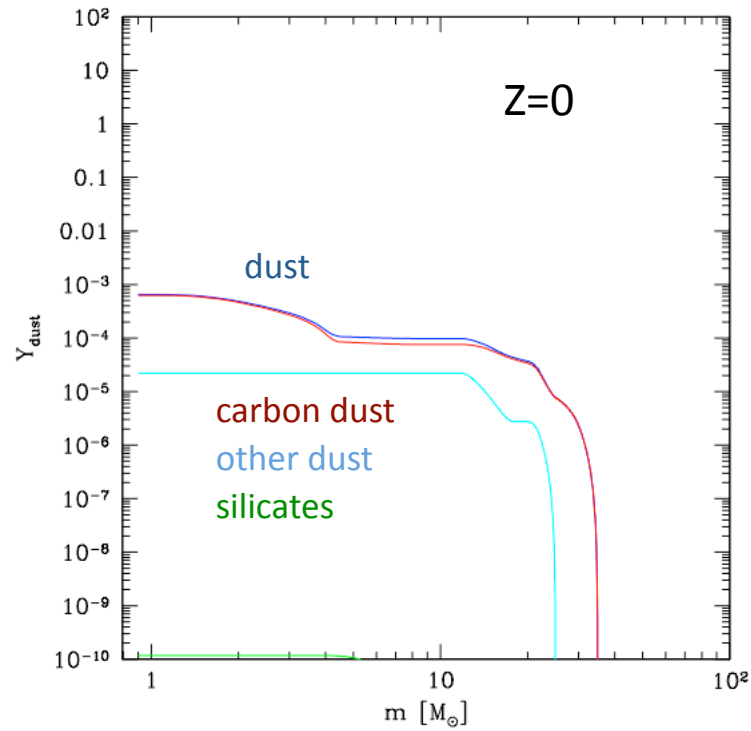


Woosley & Weaver (1995)
Van den Hoek & Groenewegen (1997)

metal yields



dust yields



Bianchi & Schneider (2007)
Zhukovska et al. (2008)

initial conditions

(1) Spherical extragalactic HII regions

Initial available gas mass, $M_{\text{gas}} = 10^7 M_{\text{sun}}$

dense = $1e5 \text{ cm}^{-3}$

compact = $3e3 \text{ cm}^{-3}$

diffuse = $1e2 \text{ cm}^{-3}$

(2) Ultra-luminous-like spherical scaled-up extragalactic HII regions:

Initial available gas mass, $M_{\text{gas}} = 10^9 M_{\text{sun}}$

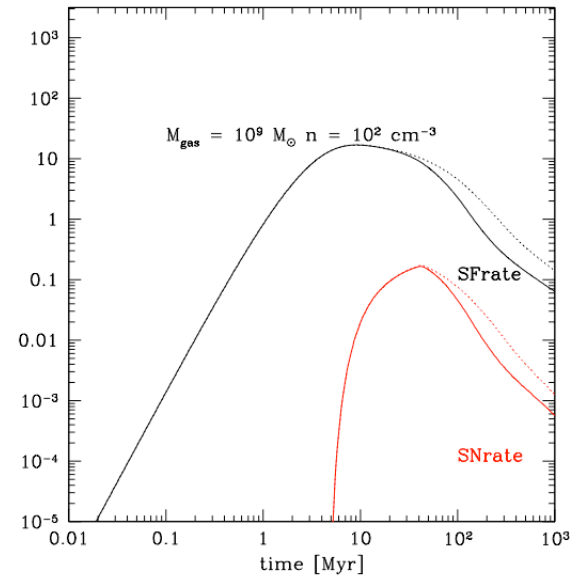
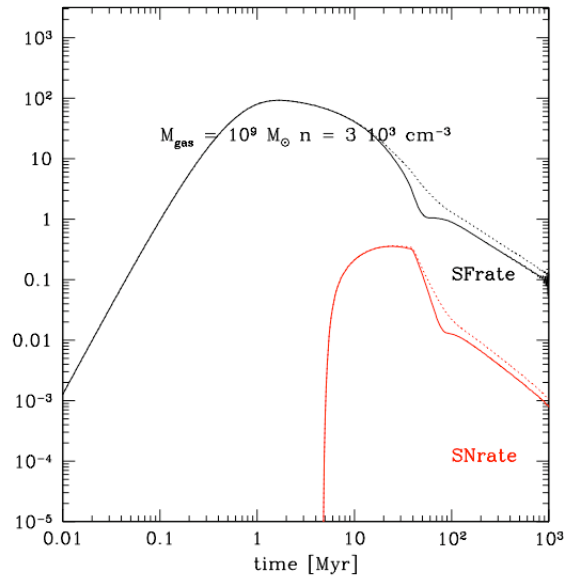
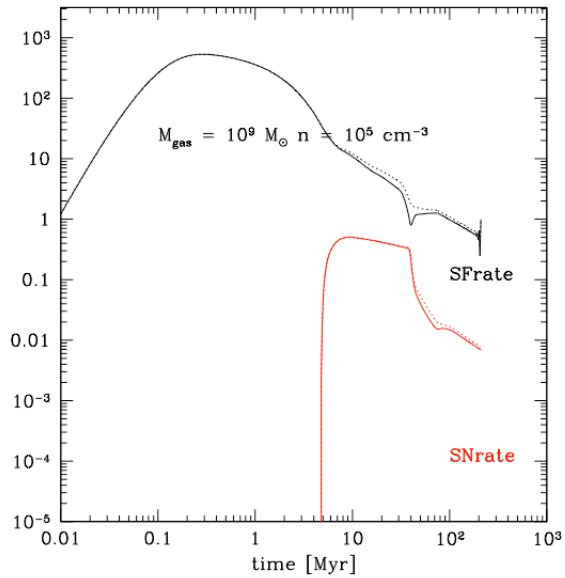
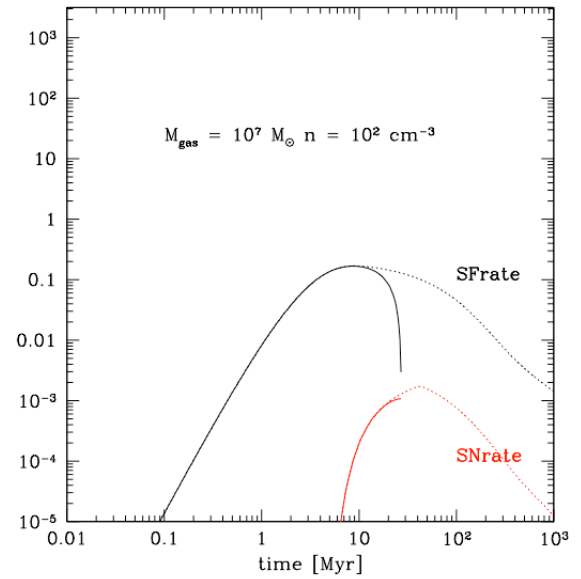
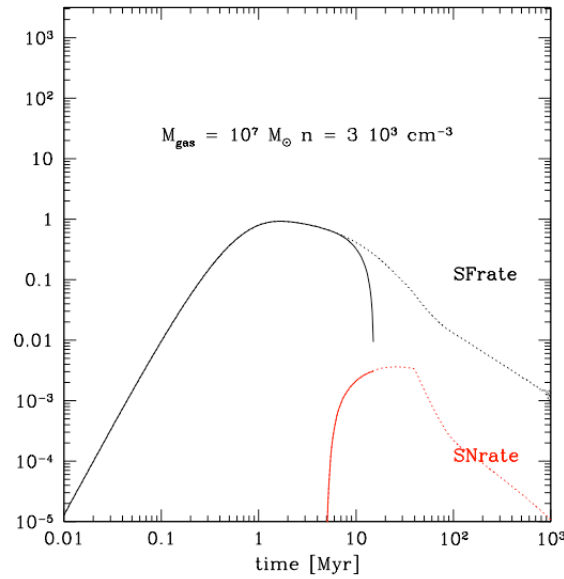
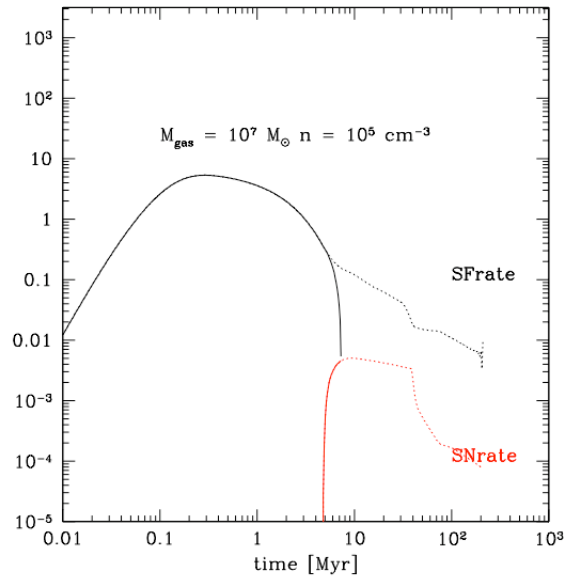
dense = $1e5 \text{ cm}^{-3}$

compact = $3e3 \text{ cm}^{-3}$

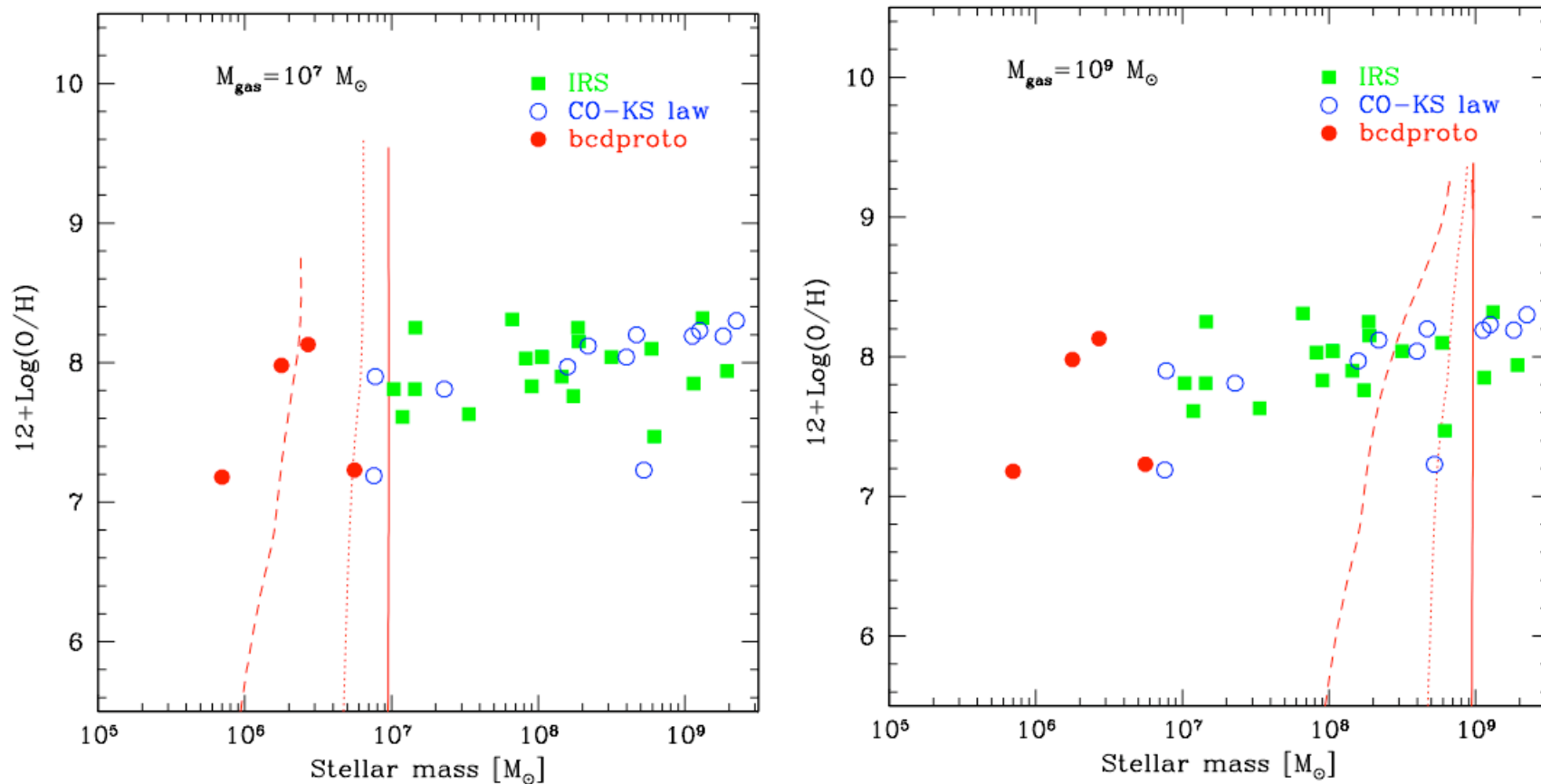
diffuse = $1e2 \text{ cm}^{-3}$

$$\text{SFR} = \text{eff} * M_{\text{gas}} / t_{\text{ff}} \text{ with eff} = 0.1$$

star formation histories & SN rate

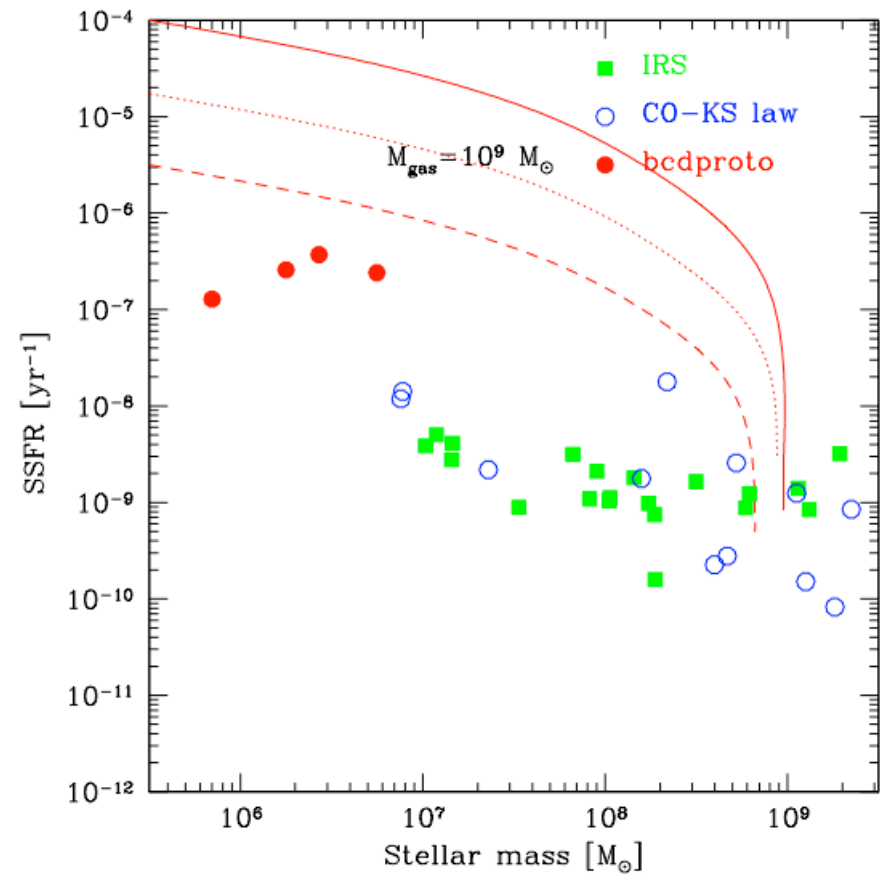
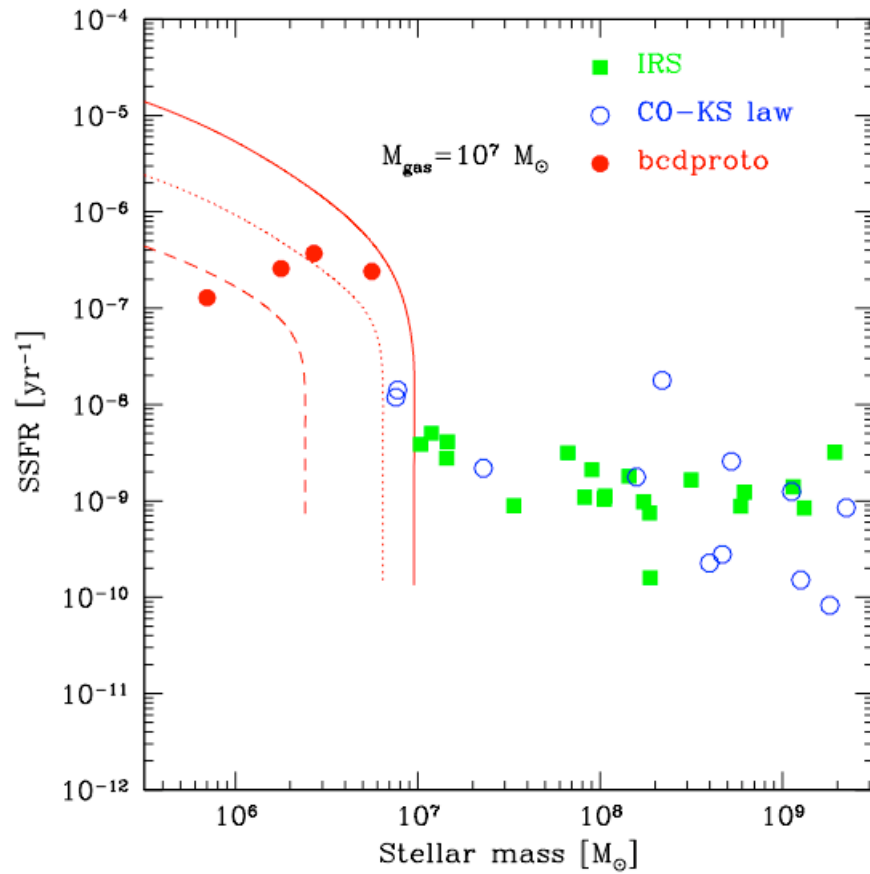


Mass-metallicity relation



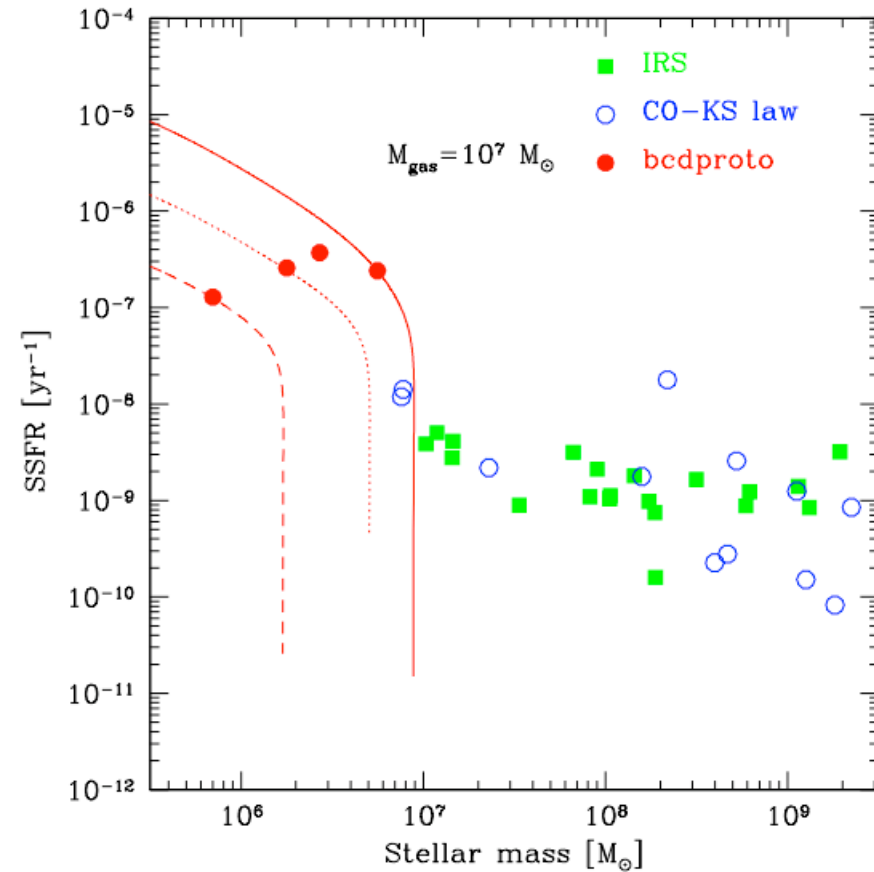
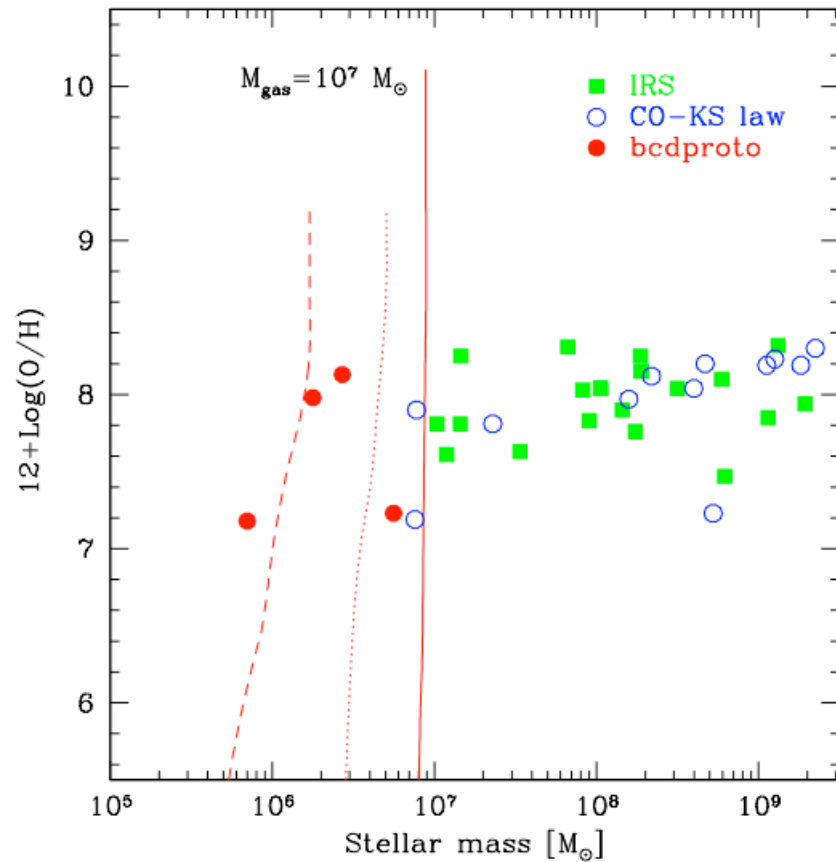
- compact
- ⋯ dense
- - - diffuse

Specific star formation rate



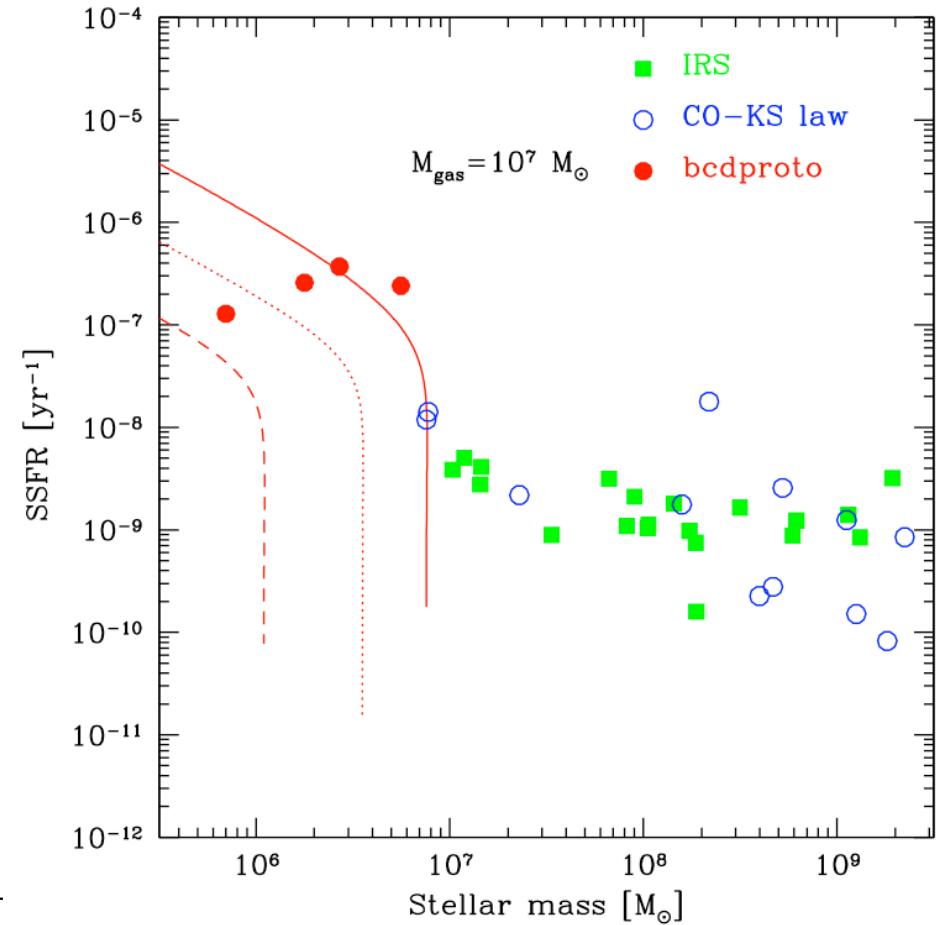
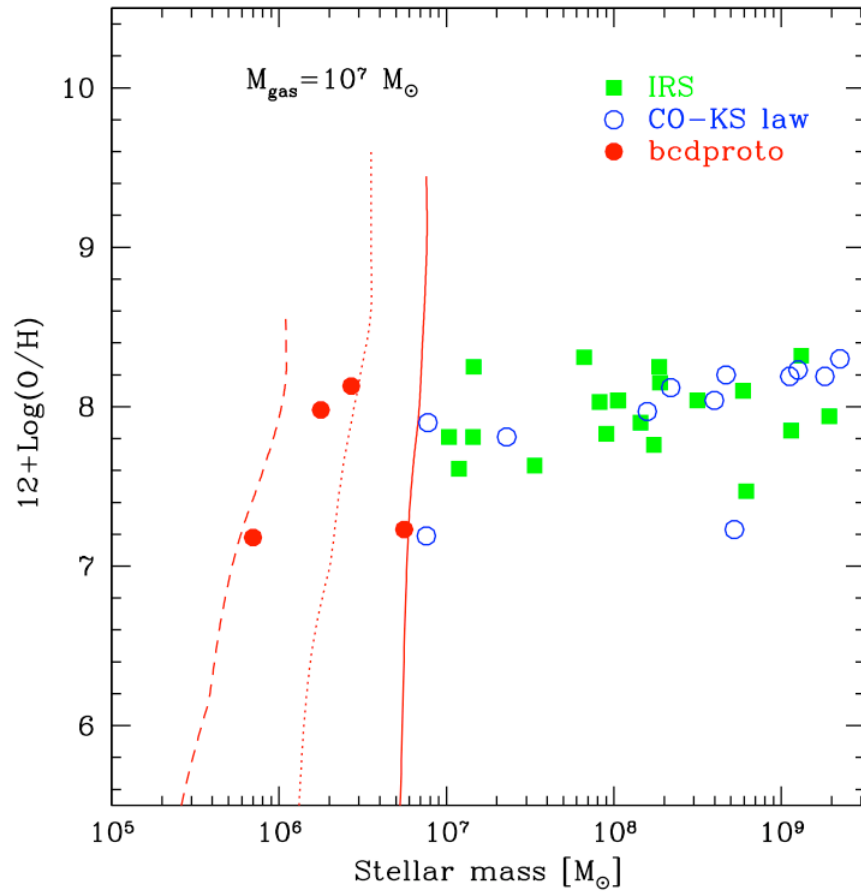
- compact
- ⋯ dense
- - - diffuse

With reduced efficiency (0.05)



- compact
- dense
- - - diffuse

With reduced efficiency (0.02)



- compact
- ⋯ dense
- - - diffuse

New SFR prescription

Stars form out of molecular gas

$$\text{SFR} = \epsilon f_{\text{H}_2} M_{\text{gas}} / t_{\text{ff}}$$

$$\epsilon = 0.01$$

fraction of molecular gas:
depends on physical conditions

free-fall time within the
molecular cloud

$$f_{\text{H}_2} = f_{\text{H}_2}(Z_{\text{met}}, \Sigma_{\text{gas}})$$

Krumholz, McKee & Tumlinson (2009)

surface density of the atomic/molecular complex

$$\Sigma_{\text{gas}} = \Sigma_{\text{H}_2} + \Sigma_{\text{HI}}$$

$$\Sigma_{\text{H}_2} = N_{\text{cl}} \Sigma_{\text{cl}} \quad \Sigma_{\text{cl}} = 85 M_{\text{sun}} / \text{pc}^2$$

$$N_{\text{cl}} = M_{\text{H}_2} / M_{\text{cl}}$$

$$M_{\text{cl}} = M_{\text{jeans}}(n_{\text{HI}}, T_{\text{HI}}) = 1660 M_{\text{sun}} (T_{\text{HI}} / 25\text{K})^{3/2} n_{\text{HI}}^{-1/2}$$

Initial Conditions

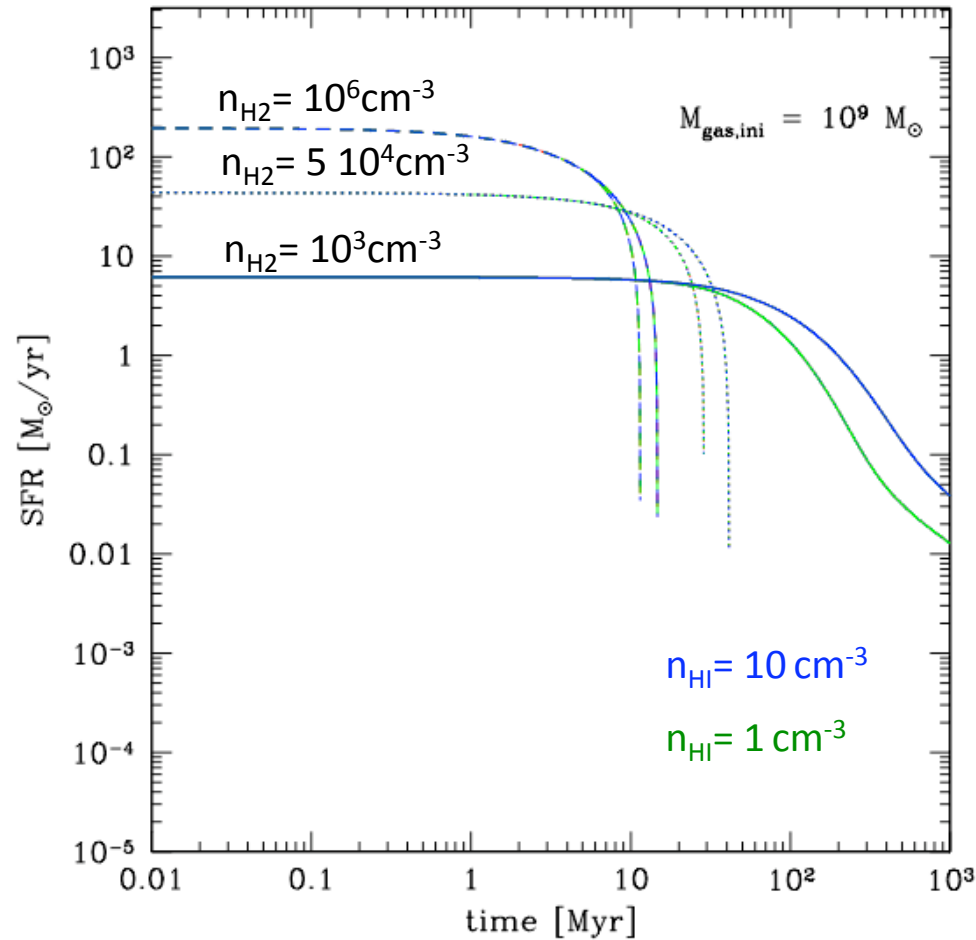
$$M_{\text{gas}} = 10^9, 10^{11} M_{\text{sun}}$$

$$T_{\text{HI}} = 20, 25, 30 \text{ K}$$

$$n_{\text{HI}} = 1, 10 \text{ cm}^{-3}$$

$$n_{\text{H}_2} = 10^3, 5 \cdot 10^4, 10^6 \text{ cm}^{-3}$$

star formation histories (no infall)

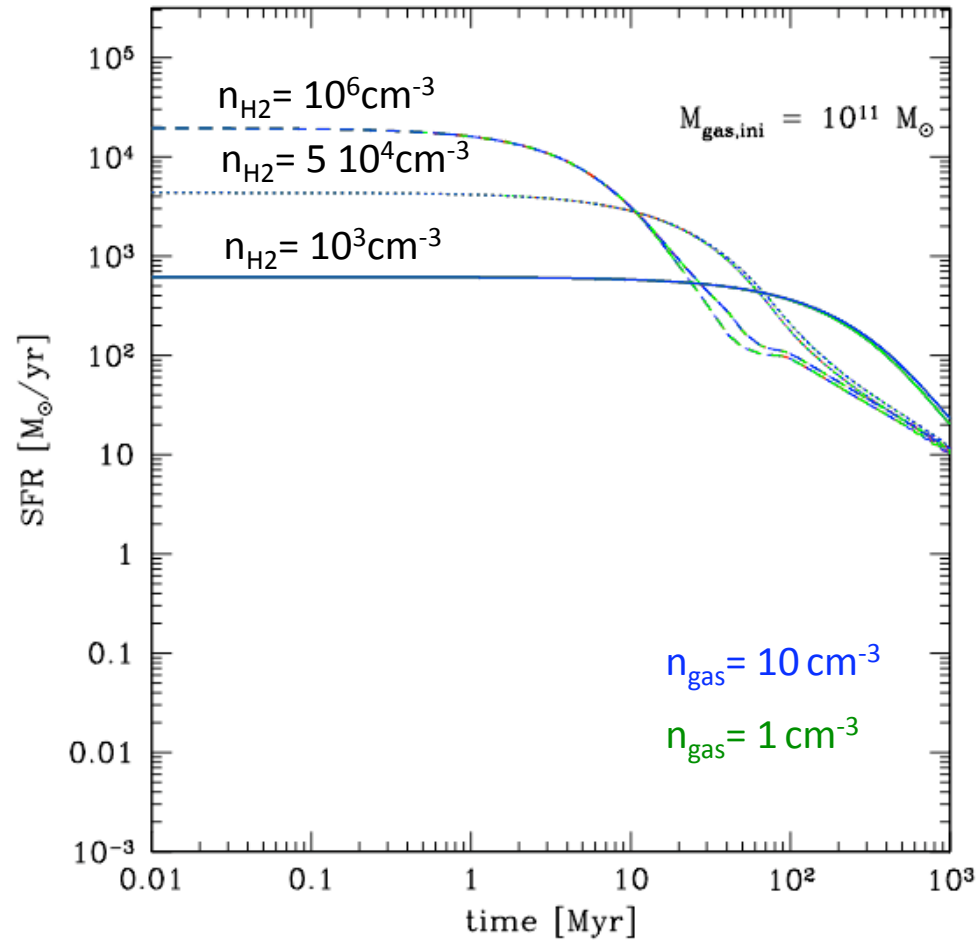


$$M_{\text{gas,ini}} = 10^9 M_{\text{sun}}$$

$$\text{SFR} = \epsilon f_{\text{H}_2} M_{\text{gas}}/t_{\text{ff}}$$

SFR depends on n_{HI} only through the strength of SN feedback (fix E_b and v_{esc})

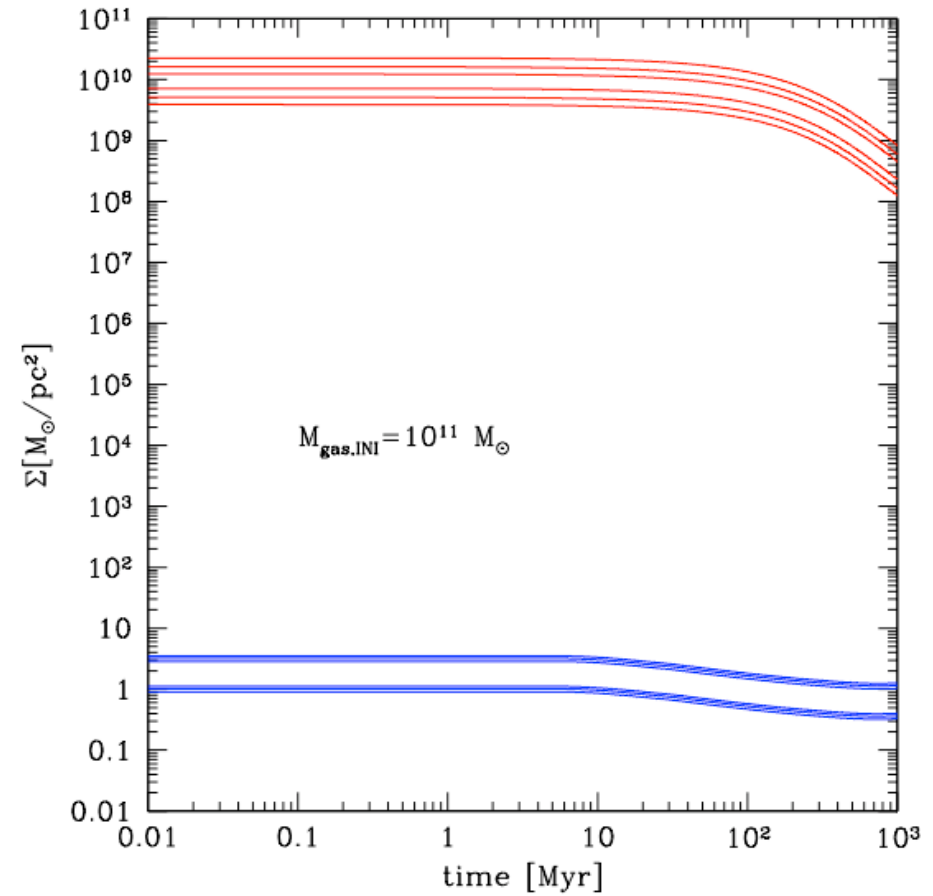
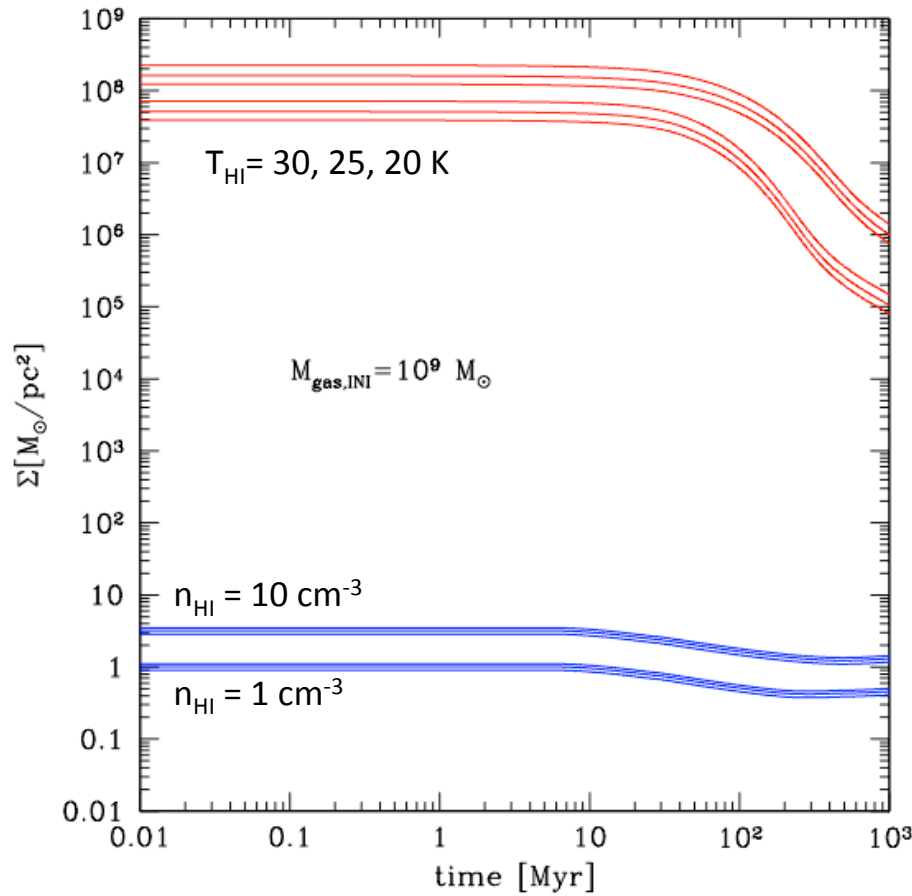
star formation histories (no infall)



$$M_{\text{gas,ini}} = 10^{11} M_{\text{sun}}$$

$$\text{SFR} = \epsilon f_{\text{H}_2} M_{\text{gas}}/t_{\text{ff}}$$

Problem: after 1 step $f_{\text{H}_2}=1$



$$\Sigma_{\text{gas}} = \Sigma_{\text{H}_2} + \Sigma_{\text{HI}}$$

$$\Sigma_{\text{H}_2} = N_{\text{cl}} \Sigma_{\text{cl}}$$

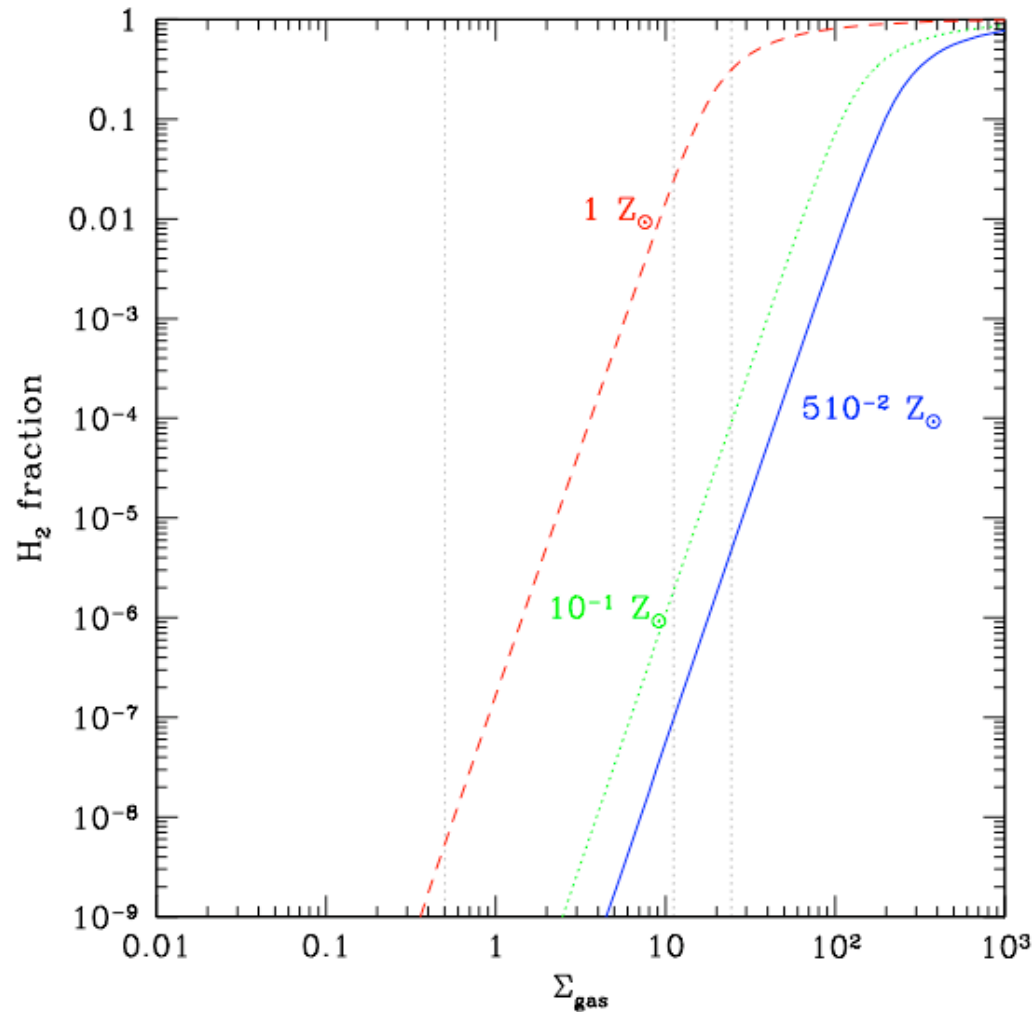
$$M_{\text{H}_2} = f_{\text{h}_2}(\Sigma_{\text{gas}}, Z_{\text{gas}})$$

$$N_{\text{cl}} = M_{\text{H}_2}/M_{\text{cl}}$$

$$M_{\text{cl}} = M_{\text{jeans}}(n_{\text{HI}}, T_{\text{HI}}) = 1660 M_{\text{sun}} (T_{\text{HI}}/25\text{K})^{3/2} n_{\text{HI}}^{-1/2}$$

$$f_{\text{H}_2}(\Sigma_{\text{gas}}, Z)$$

Krumholz, McKee, Tumlinson 2009



@ t_{ini}, M_{H₂}=0 and Σ_{gas} = Σ_{HI} f_{H₂} ≈ 10⁻⁴

@ t_{ini} + Δt, M_{H₂} ≈ 10⁵ M_{sun} and N_{cl} >> 1
 Σ_{gas} = Σ_{H₂} >> 10² M_{sun}/pc² f_{H₂} ≈ 1 thereafter

2 problems

1. we are giving the system all the raw material at the first step → we have to re-introduce the infall term (easy!)
2. we are computing f_{H_2} using the **total** gas column density; KMT09 say that f_{H_2} depends on the column density of the atomic/molecular complex averaged over 100 pc

$$\Sigma_{\text{compl}} = c \Sigma_{\text{gas}} \text{ with } c = \text{clumping factor } (> 1 \text{ for } r > 100 \text{ pc, } \approx 1 \text{ for } r \rightarrow 100 \text{ pc})$$

$$\Sigma_{\text{cl}} = 85 M_{\text{sun}}/\text{pc}^2 \text{ if } \Sigma_{\text{gas}} < 85 M_{\text{sun}}/\text{pc}^2$$

$$\Sigma_{\text{cl}} = \Sigma_{\text{gas}} \text{ if } \Sigma_{\text{gas}} > 85 M_{\text{sun}}/\text{pc}^2$$

What is the typical “size” of a molecular cloud? $R_{\text{cl}} \approx \Sigma_{\text{cl}}/(2 m_{\text{H}} n_{\text{H}_2})$

$n_{\text{H}_2} [\text{cm}^{-3}]$	10^3	$5 \cdot 10^4$	10^6
$R_{\text{cl}} [\text{pc}]$	1.7	$3.4 \cdot 10^{-2}$	$1.7 \cdot 10^{-3}$

and the “size” of the HI region? $R_{\text{HI}} = \{3 M_{\text{HI}}/4 \pi \rho_{\text{HI}}\}^{1/3}$

$M_{\text{gas,ini}} = 10^9 M_{\text{sun}}$	$n_{\text{HI}} = 1/10 [\text{cm}^{-3}]$	$M_{\text{gas,ini}} = 10^{11} M_{\text{sun}}$	$n_{\text{HI}} = 1/10 [\text{cm}^{-3}]$
$R_{\text{HI}} [\text{kpc}]$	1.99/0.93	$R_{\text{HI}} [\text{kpc}]$	9.3/4.3

Re-introducing the Infall term

$$\frac{dM_{\text{inf}}}{dt} = A \left(\frac{t}{t_{\text{inf}}} \right)^2 \exp \left(-\frac{t}{t_{\text{inf}}} \right).$$

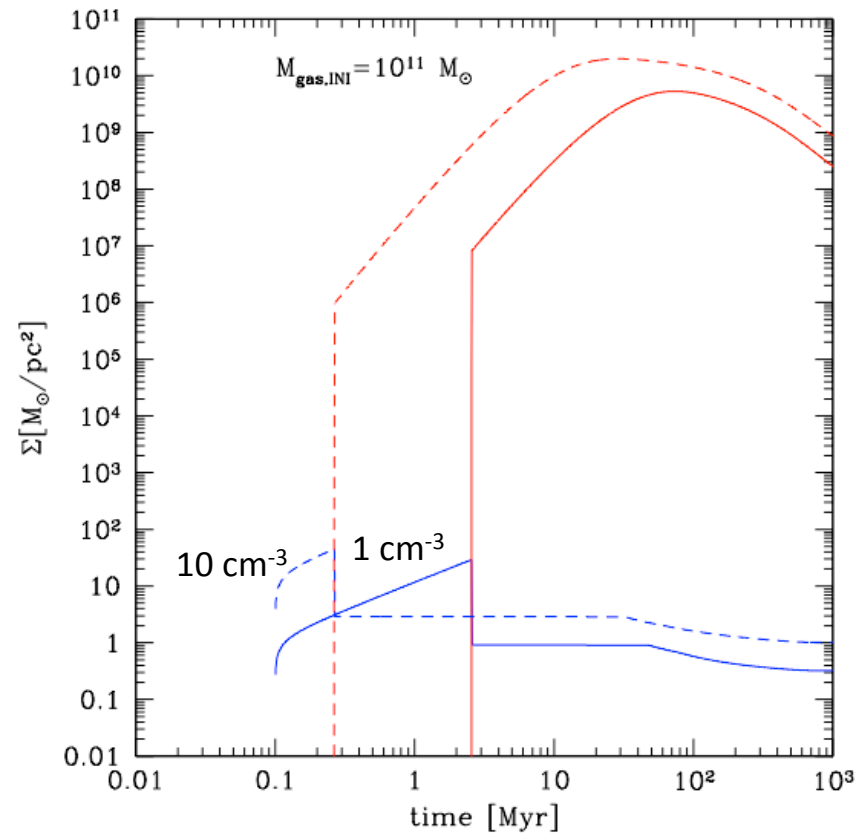
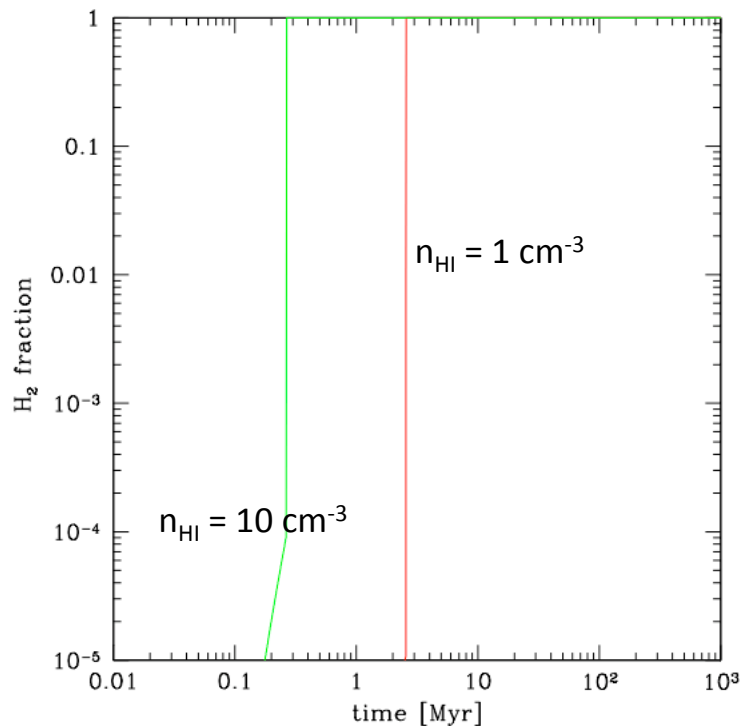
$$t_{\text{inf}} = t_{\text{ff}}/4$$

$$A = M_{\text{gas,in}}/2 t_{\text{inf}}$$

Keres et al. (2005); Salvadori et al. (2009)

Infall-time depends on the adopted HI density: $n_{\text{HI}} = 1/10 \text{ cm}^{-3}$ $t_{\text{inf}} = 12.8/4.1 \text{ Myr}$

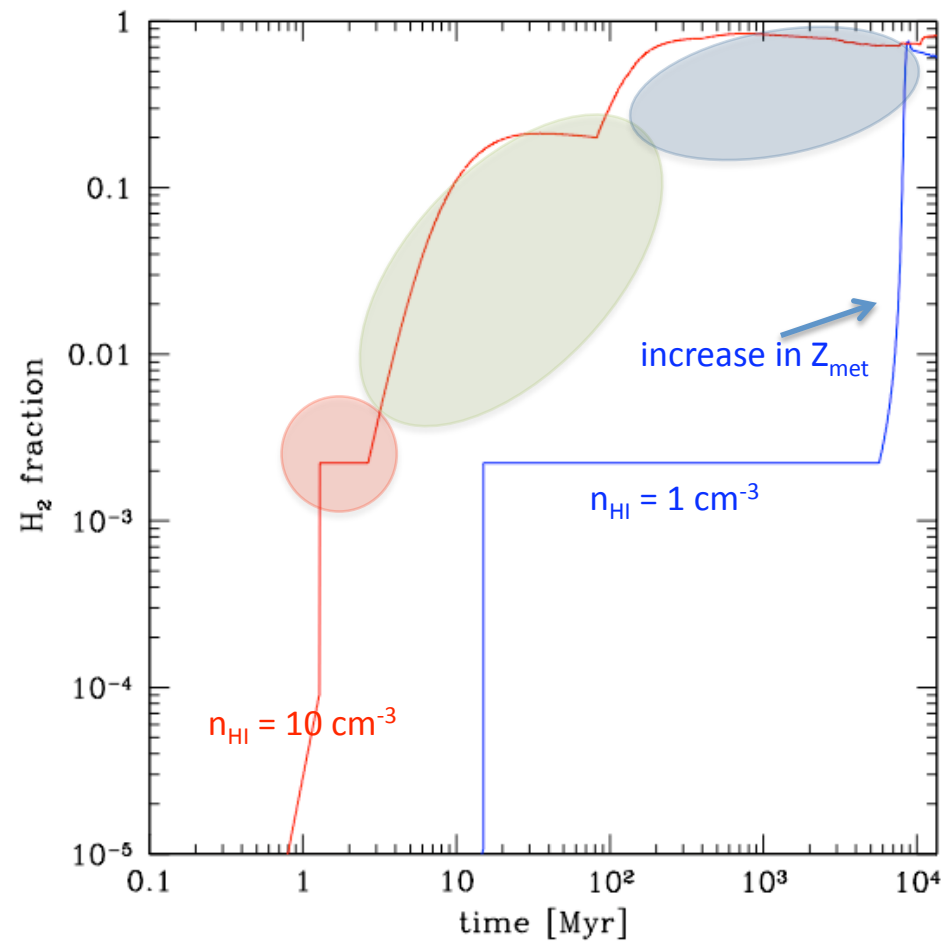
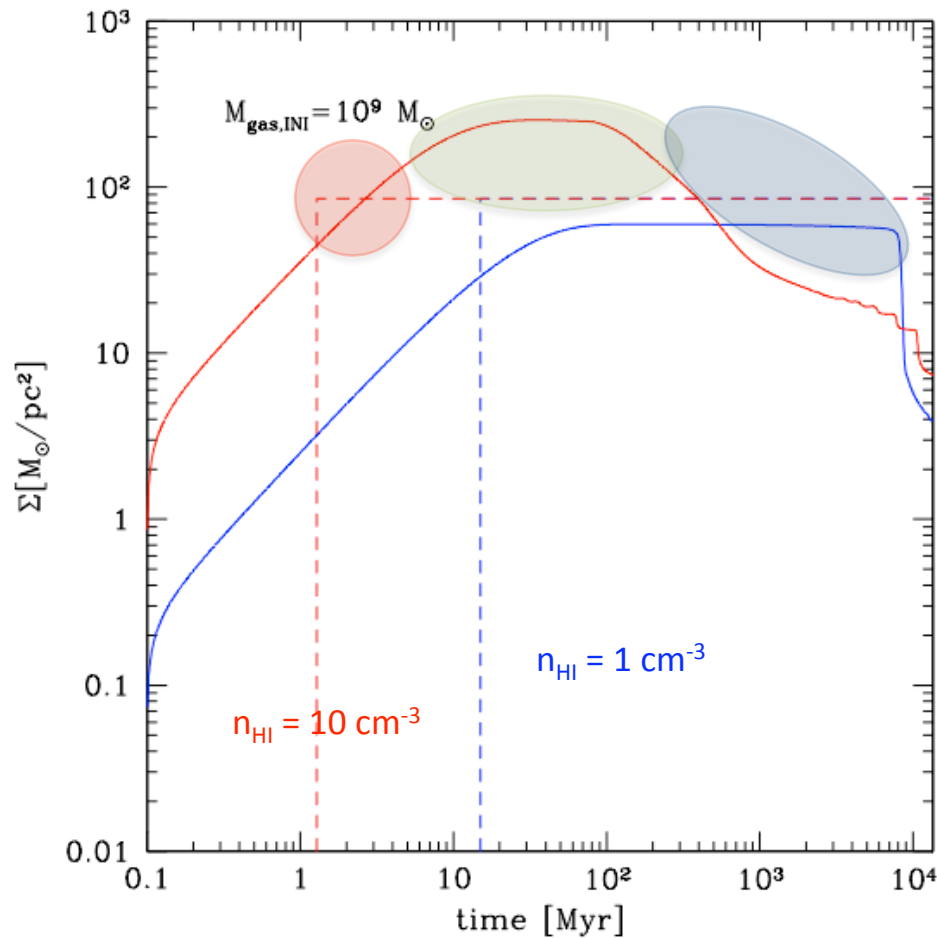
Same problem: transition is only delayed



Changing from $f_{\text{H}_2}(\Sigma_{\text{gas}})$ to $f_{\text{H}_2}(\Sigma_{\text{comp}})$

$$\Sigma_{\text{comp}} = \Sigma_{\text{HI}} \quad \text{when } N_{\text{cl}} = 0$$

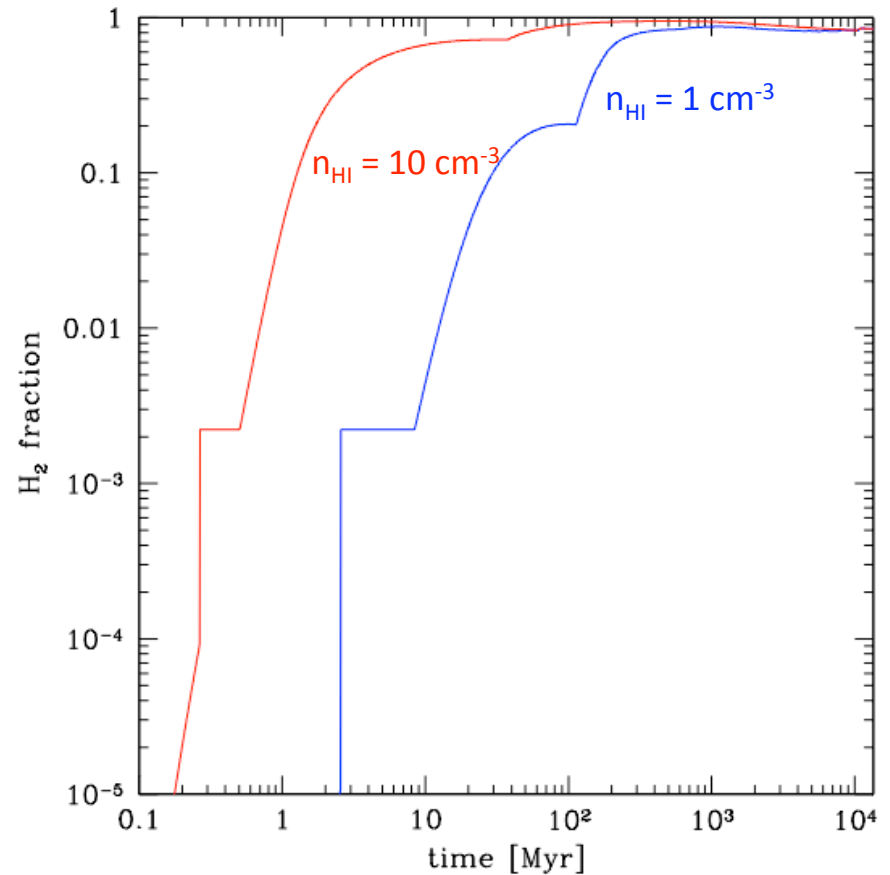
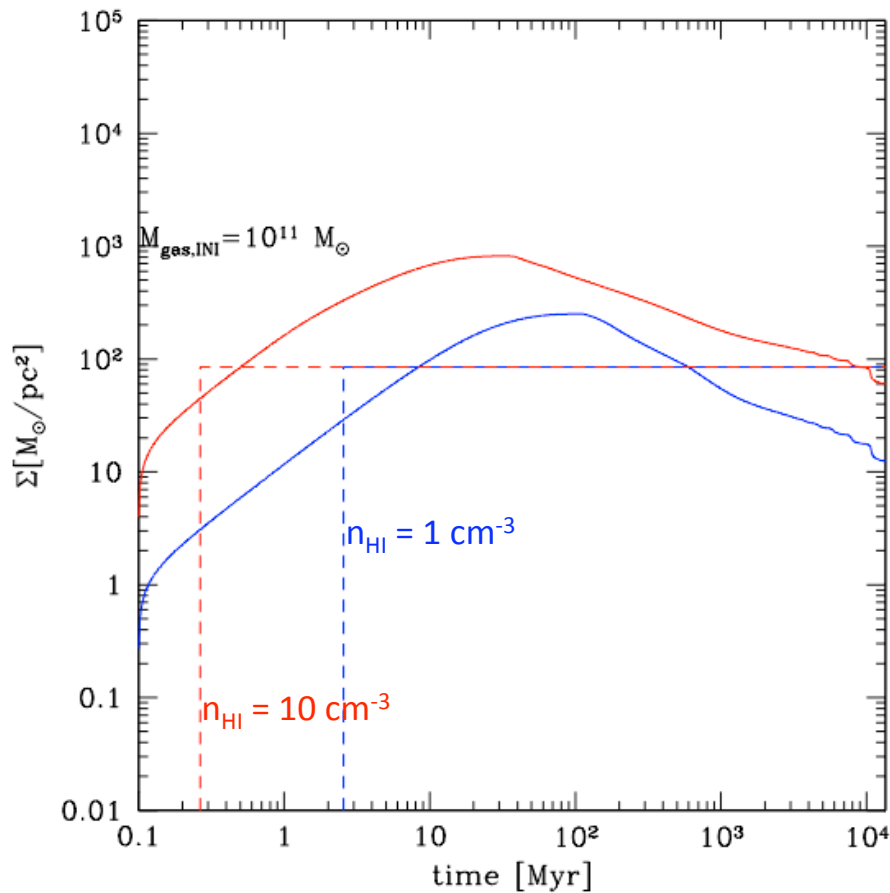
$$\Sigma_{\text{comp}} = \max(\Sigma_{\text{HI}}, \Sigma_{\text{cl}}) \quad \text{when } N_{\text{cl}} \geq 1$$



Changing from $f_{\text{H}_2}(\Sigma_{\text{gas}})$ to $f_{\text{H}_2}(\Sigma_{\text{comp}})$

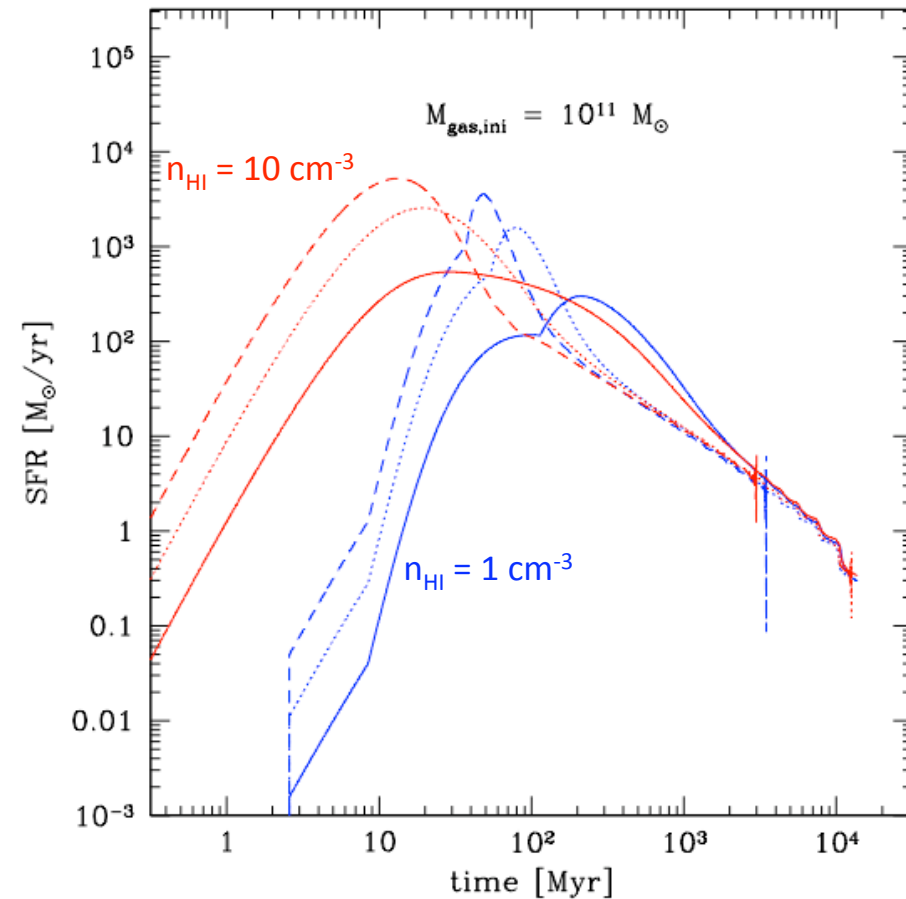
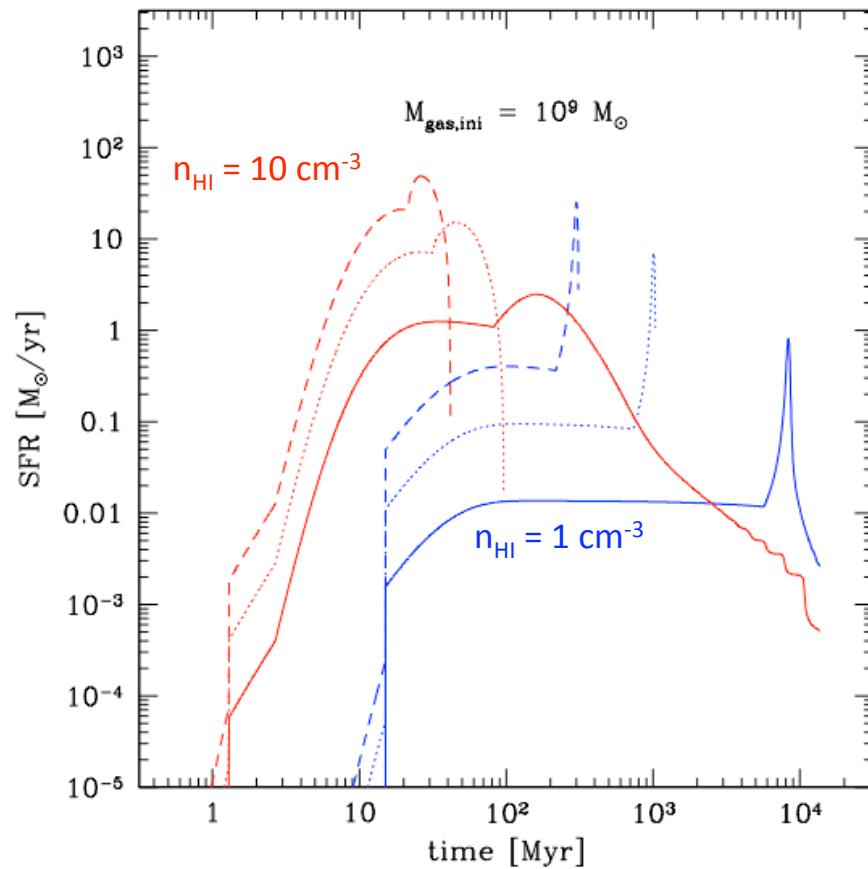
$$\Sigma_{\text{comp}} = \Sigma_{\text{HI}} \quad \text{when } N_{\text{cl}} = 0$$

$$\Sigma_{\text{comp}} = \max(\Sigma_{\text{HI}}, \Sigma_{\text{cl}}) \quad \text{when } N_{\text{cl}} \geq 1$$

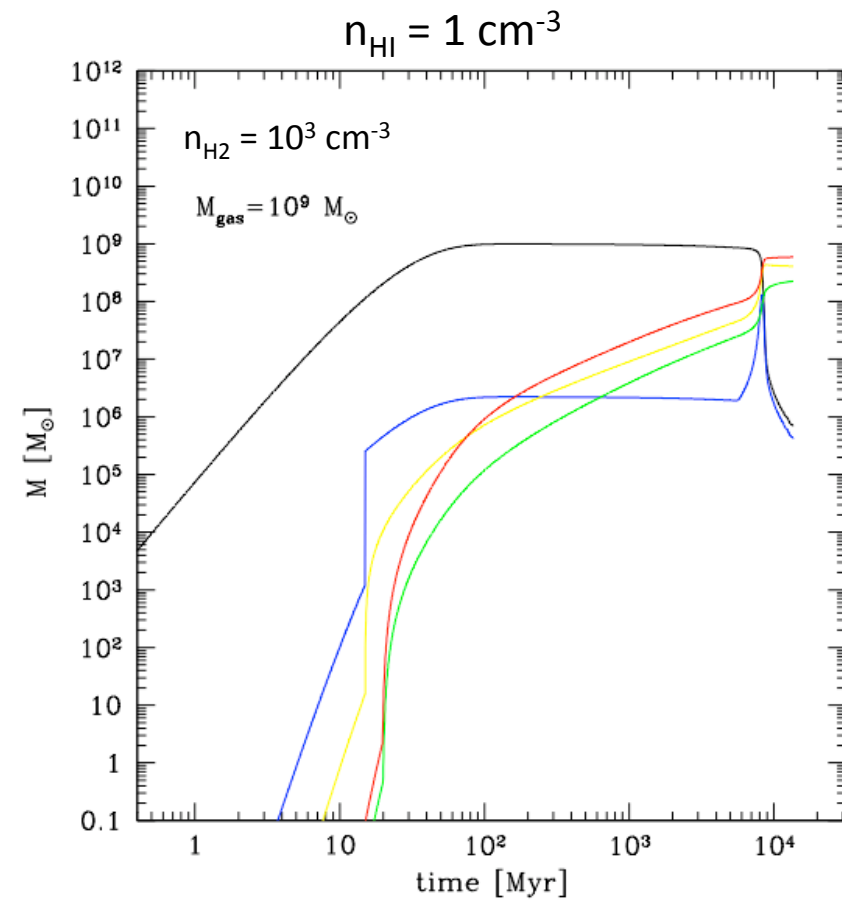
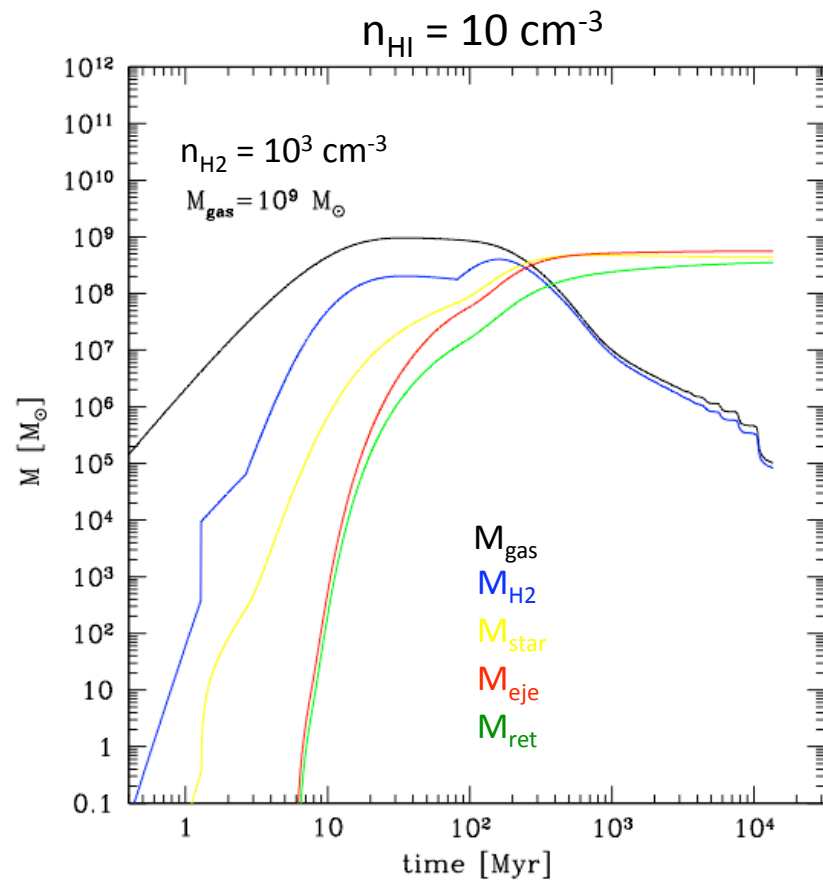


How is the SFR affected?

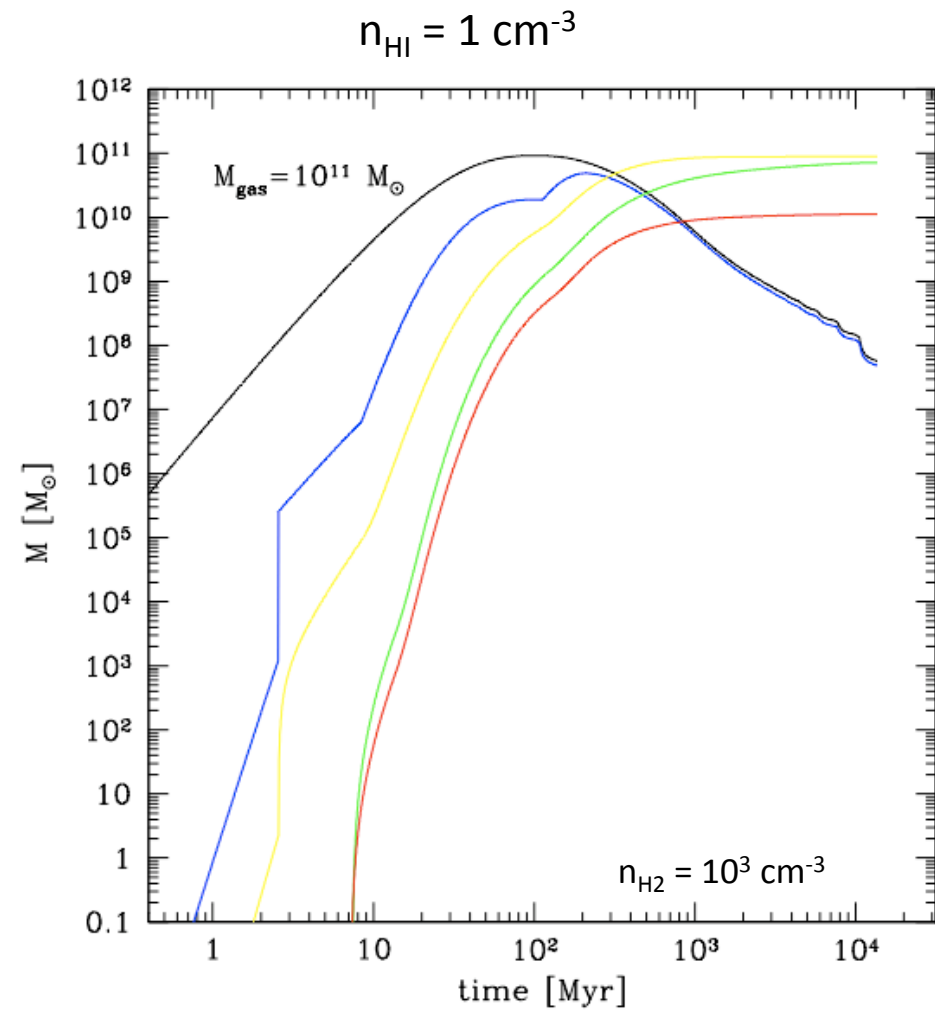
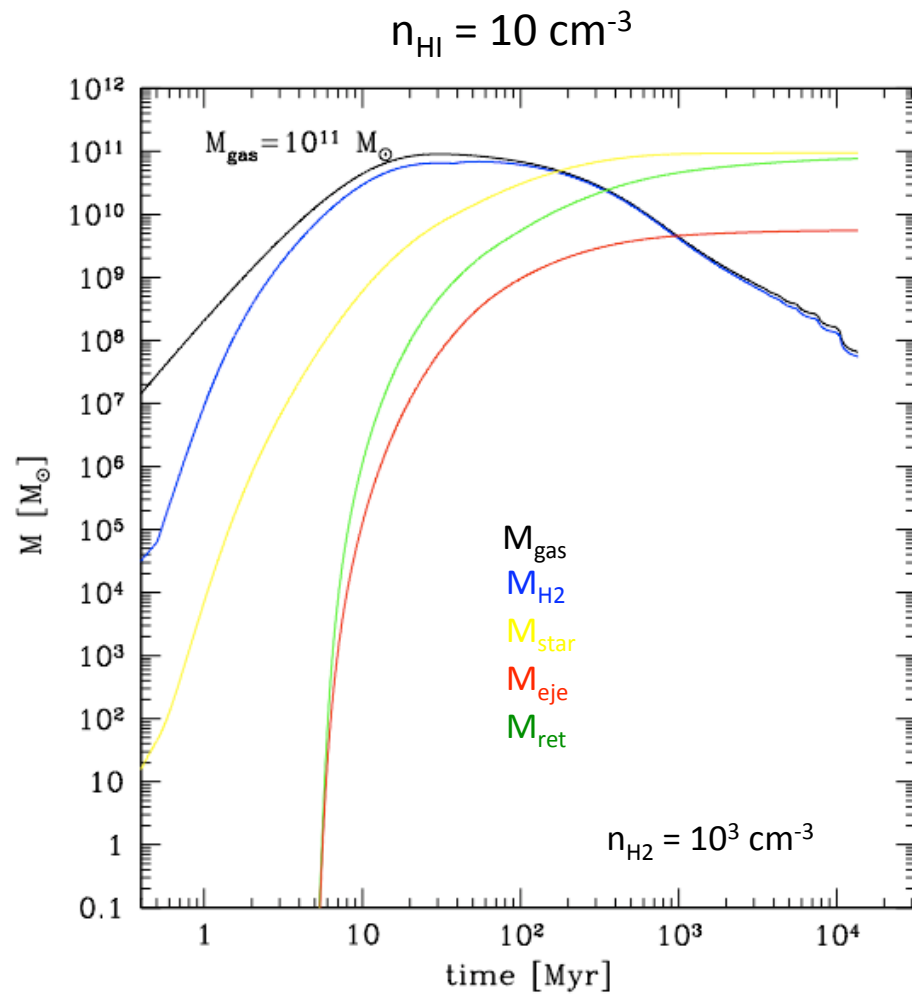
The star formation histories are very sensitive to M_{gas} and n_{HI}



time evolution: M_{gas} , M_{star} , M_{H_2}

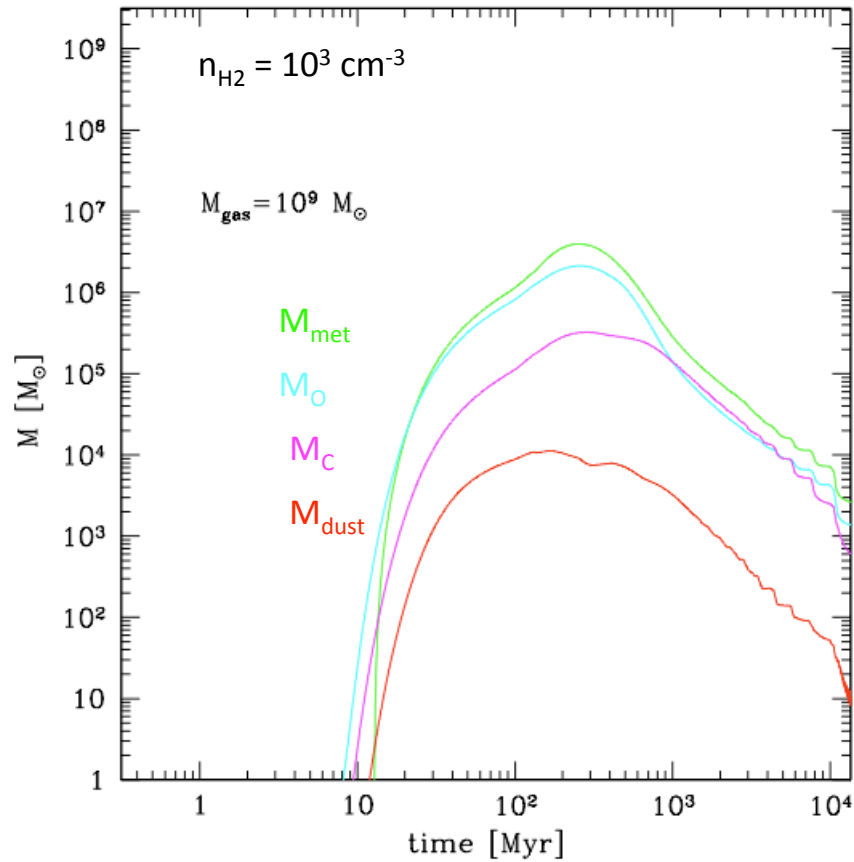


time evolution: M_{gas} , M_{star} , M_{H_2}

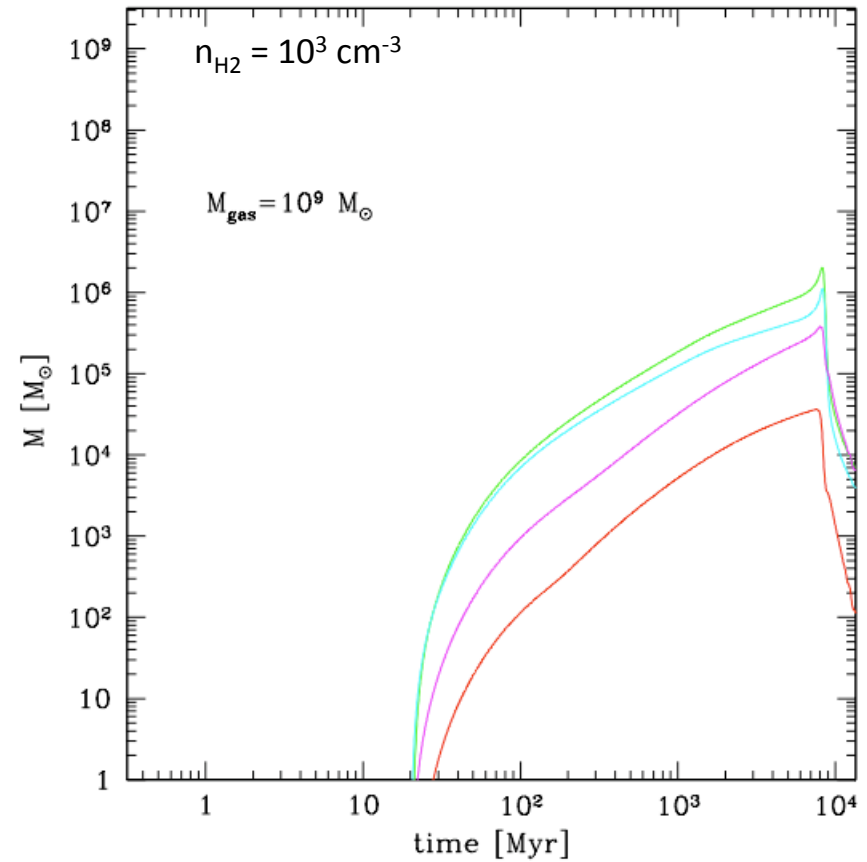


time evolution: M_{met}

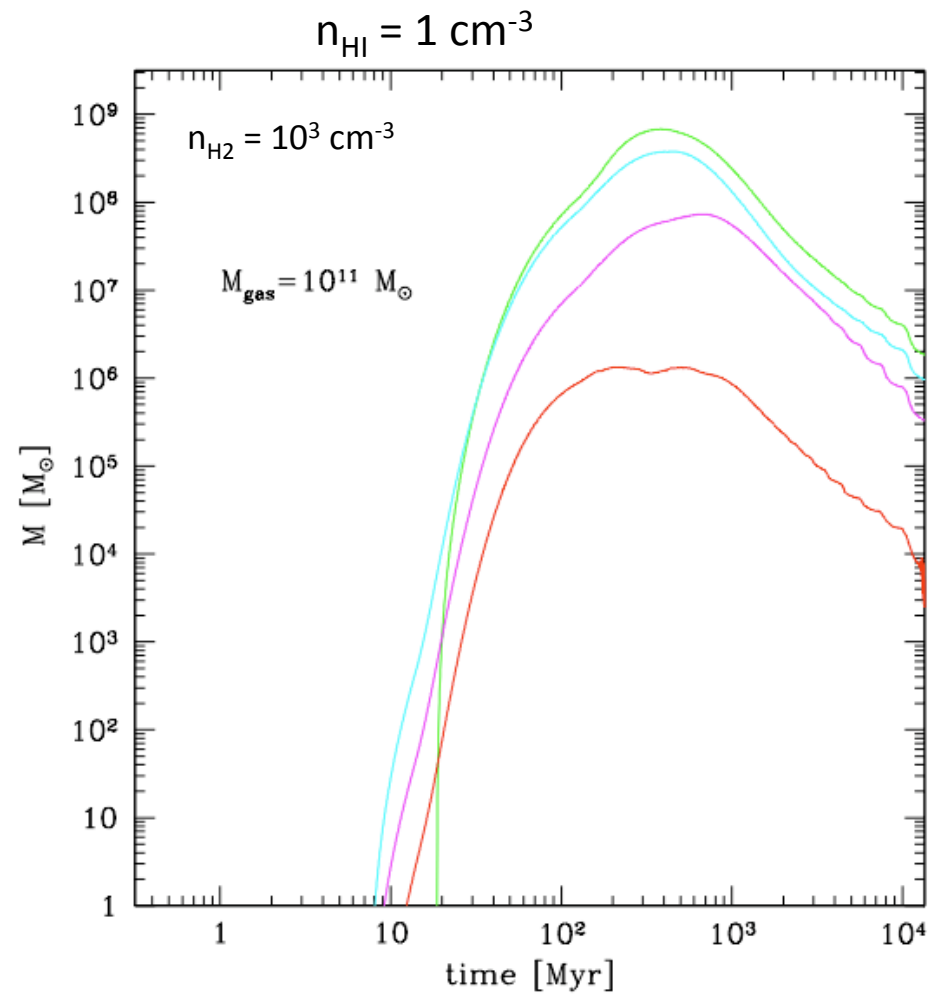
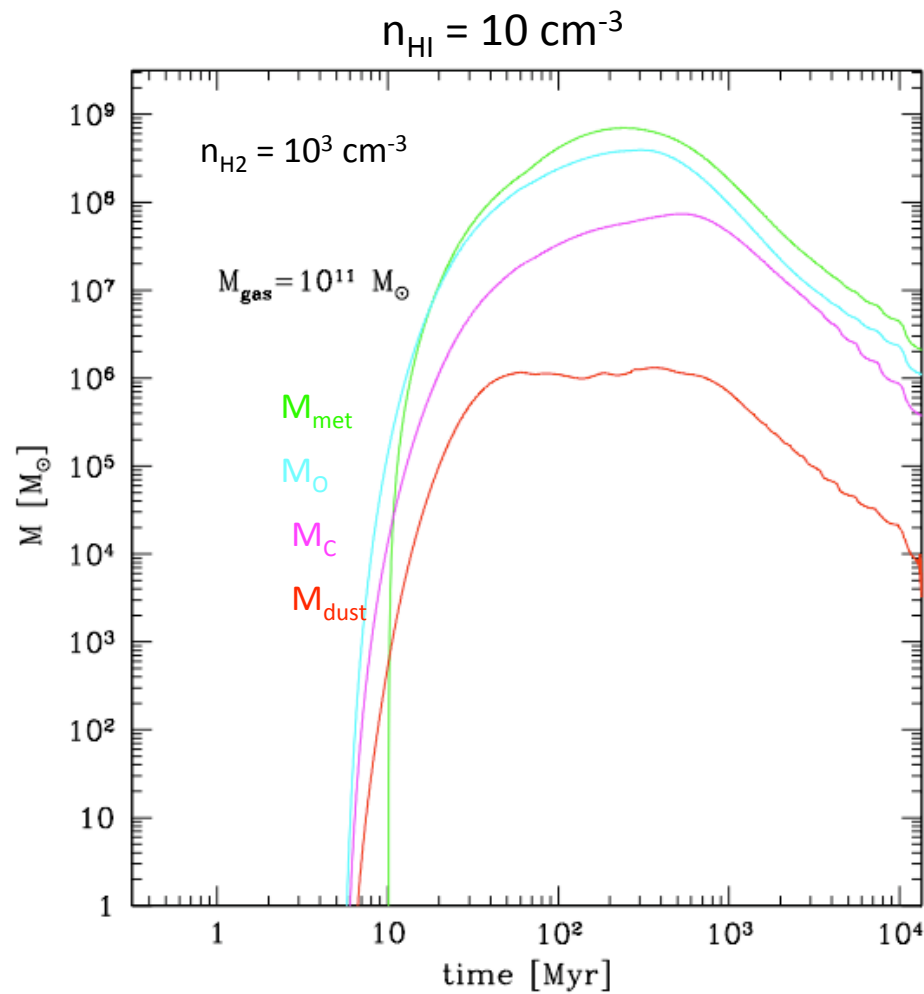
$n_{\text{HI}} = 10 \text{ cm}^{-3}$



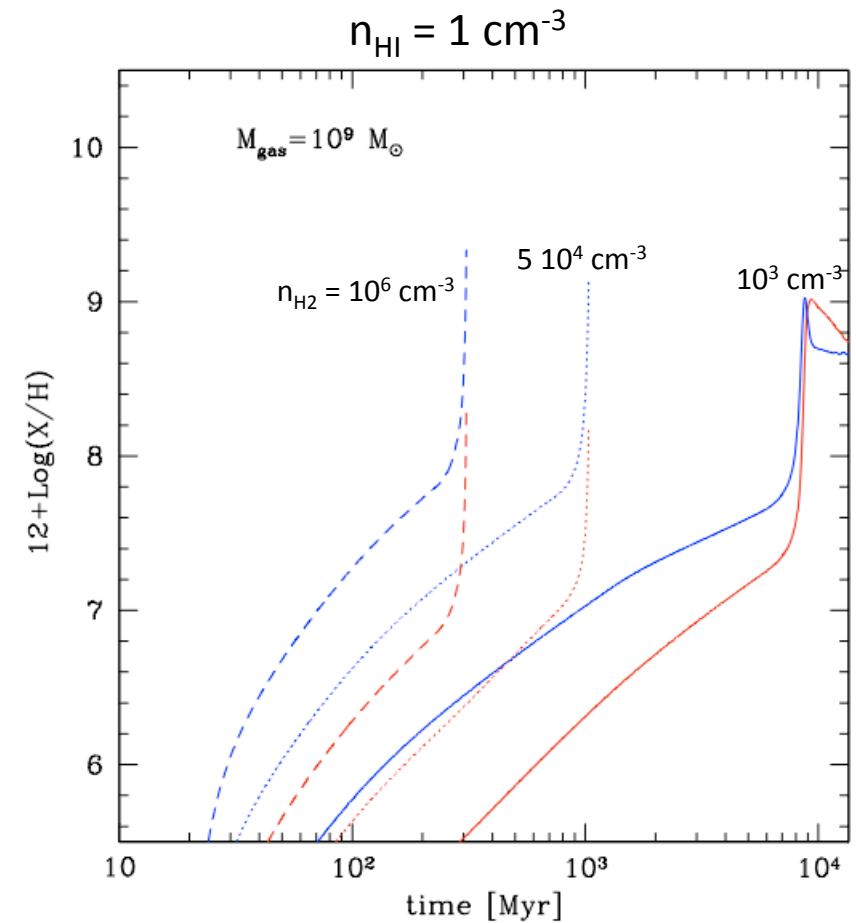
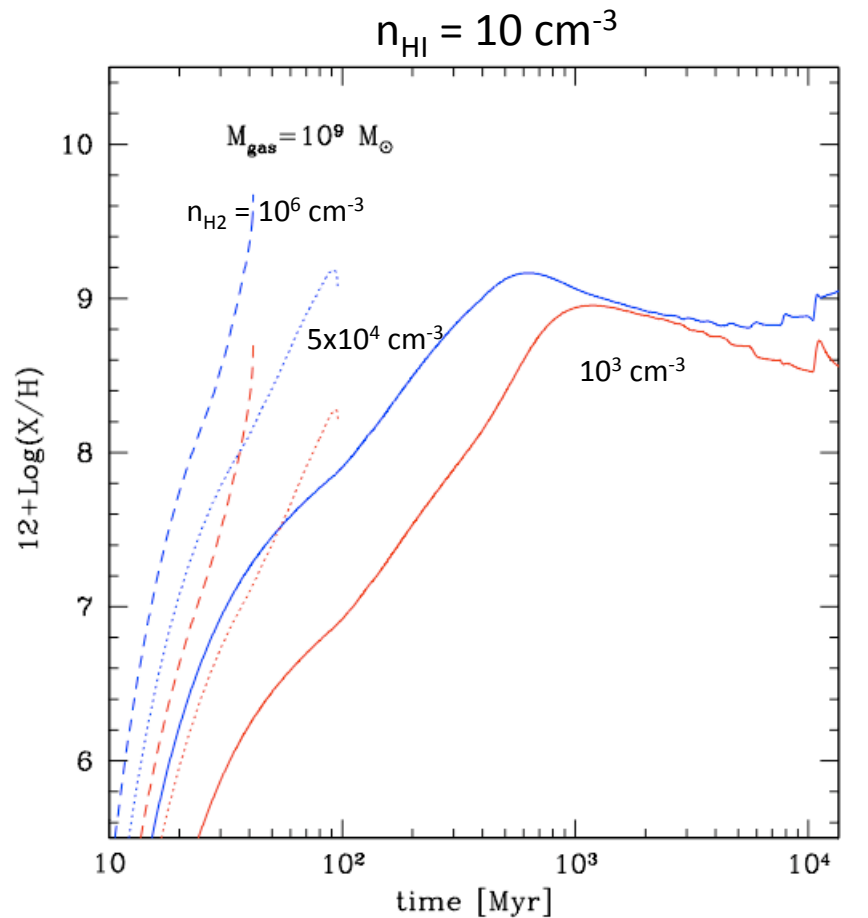
$n_{\text{HI}} = 1 \text{ cm}^{-3}$



time evolution: M_{met}

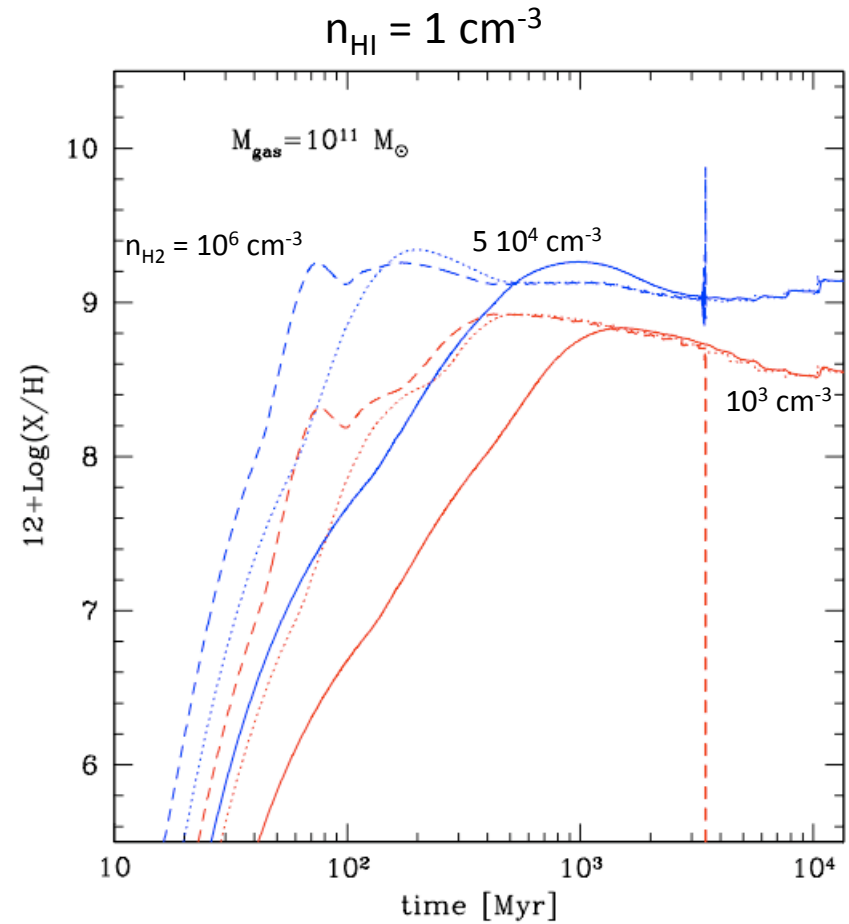
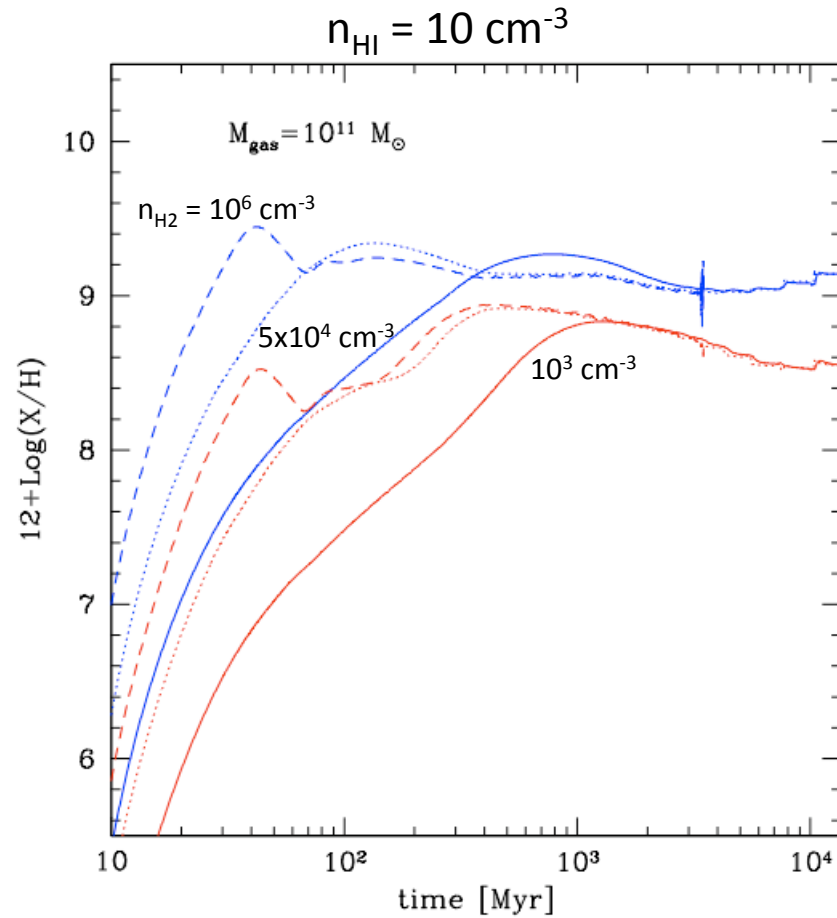


Metallicity evolution



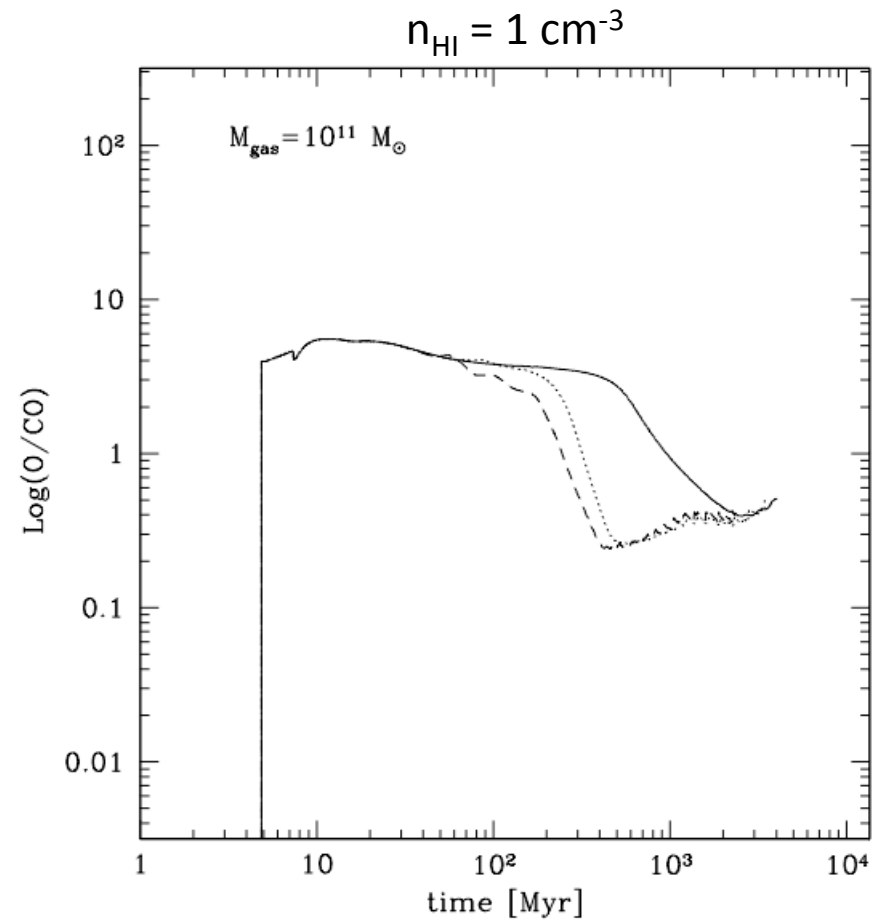
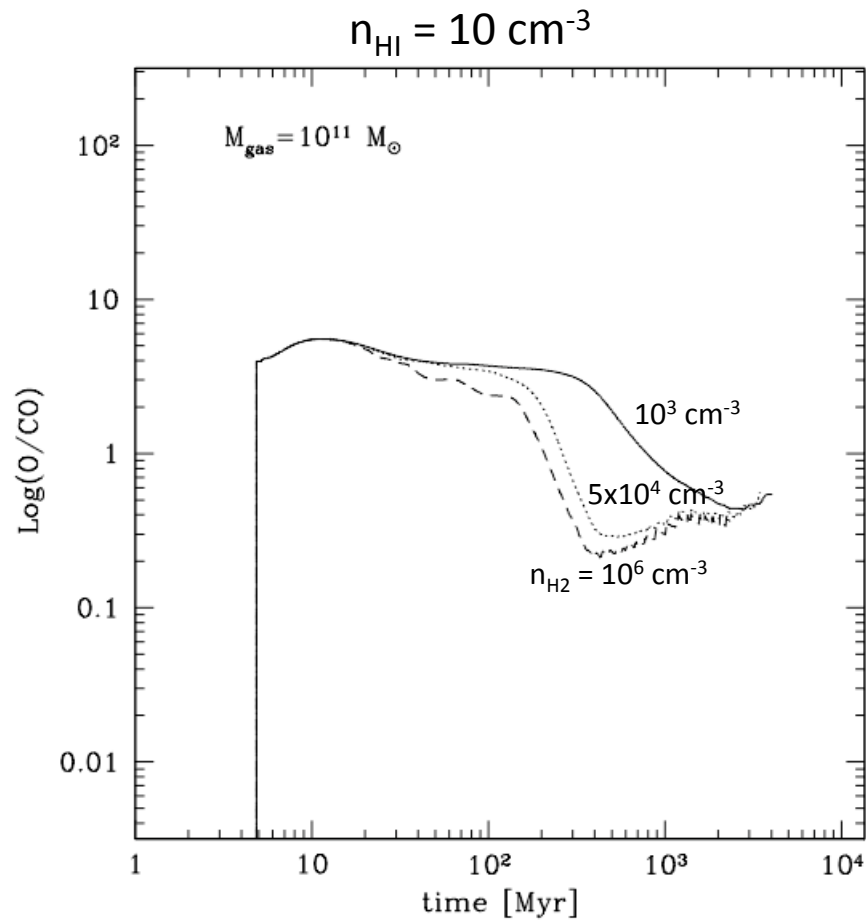
— [O/H]
— [C/H]

Metallicity evolution

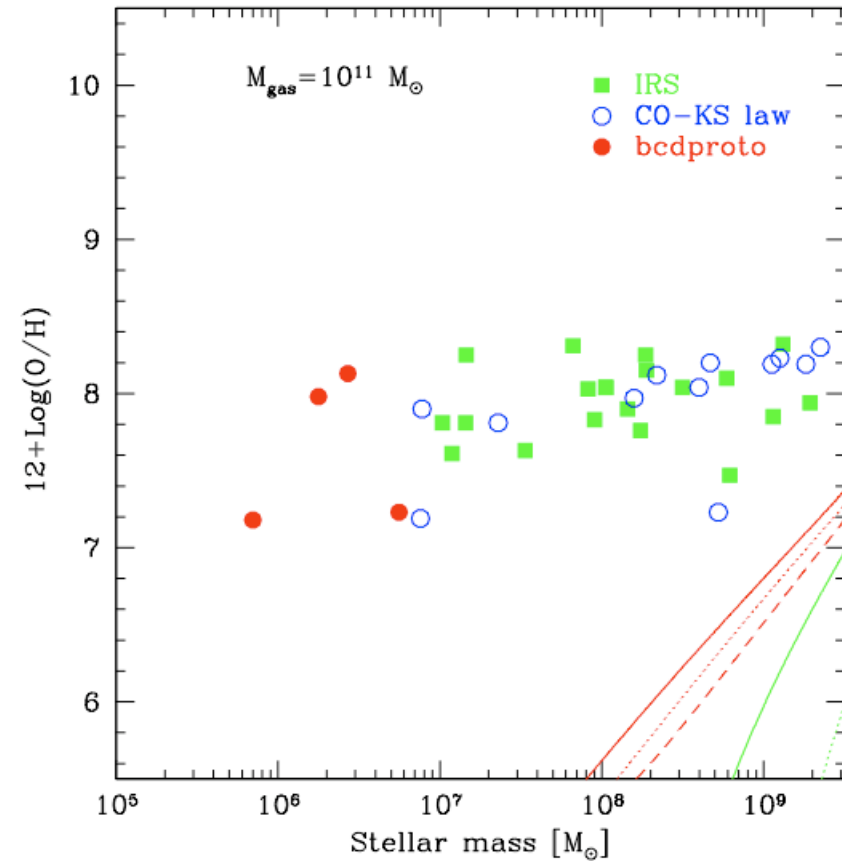
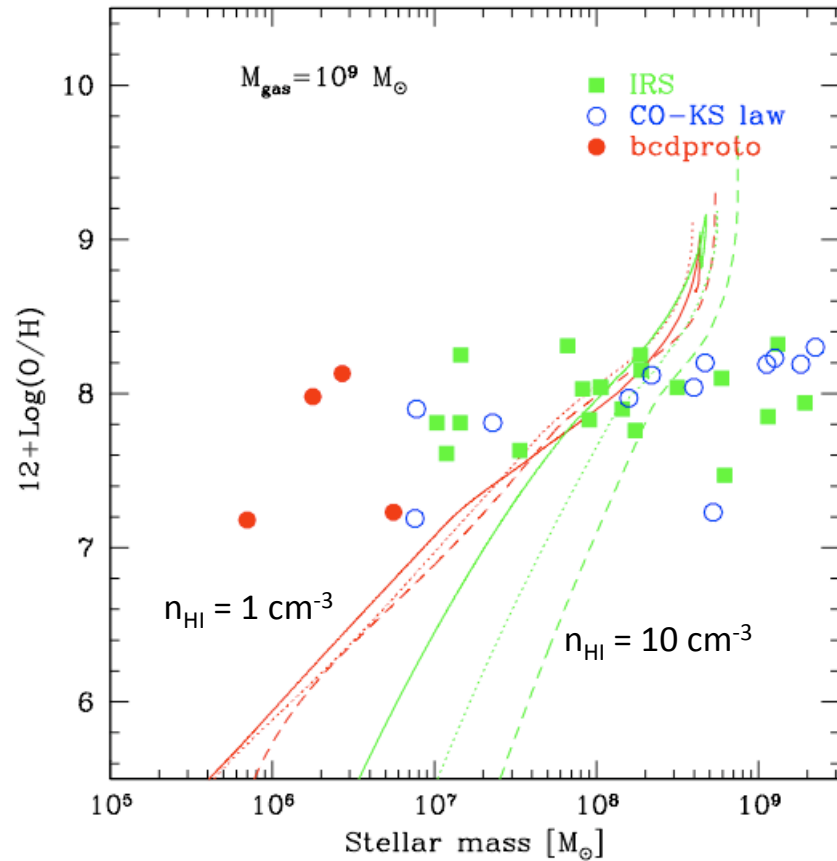


— [O/H]
— [C/H]

Molecule evolution

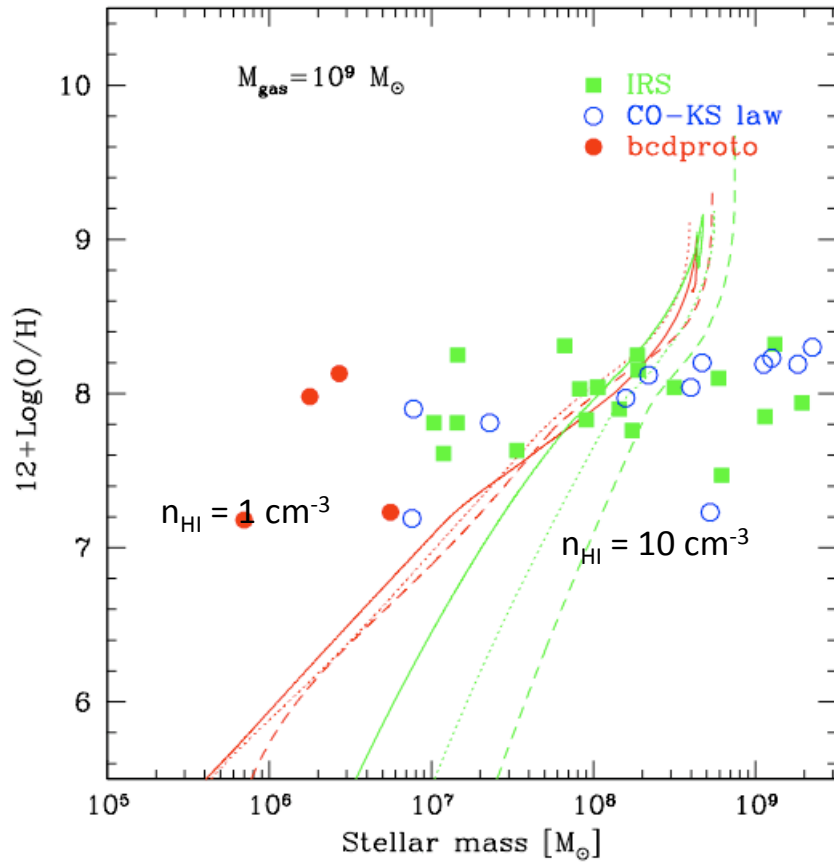


Mass-metallicity relation

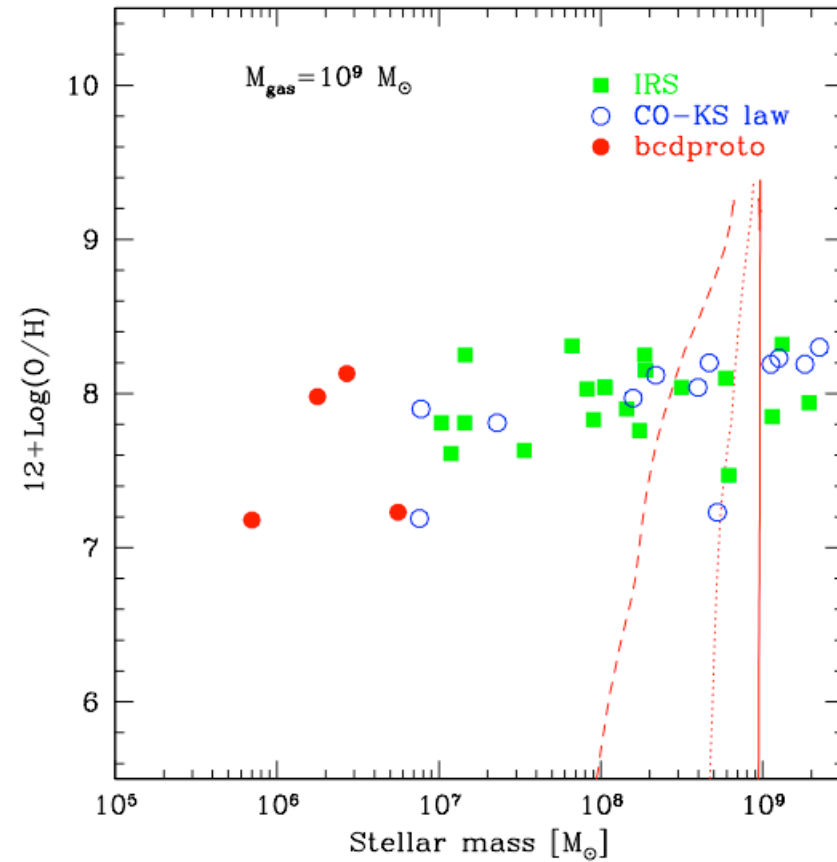


Mass-metallicity relation

New Model

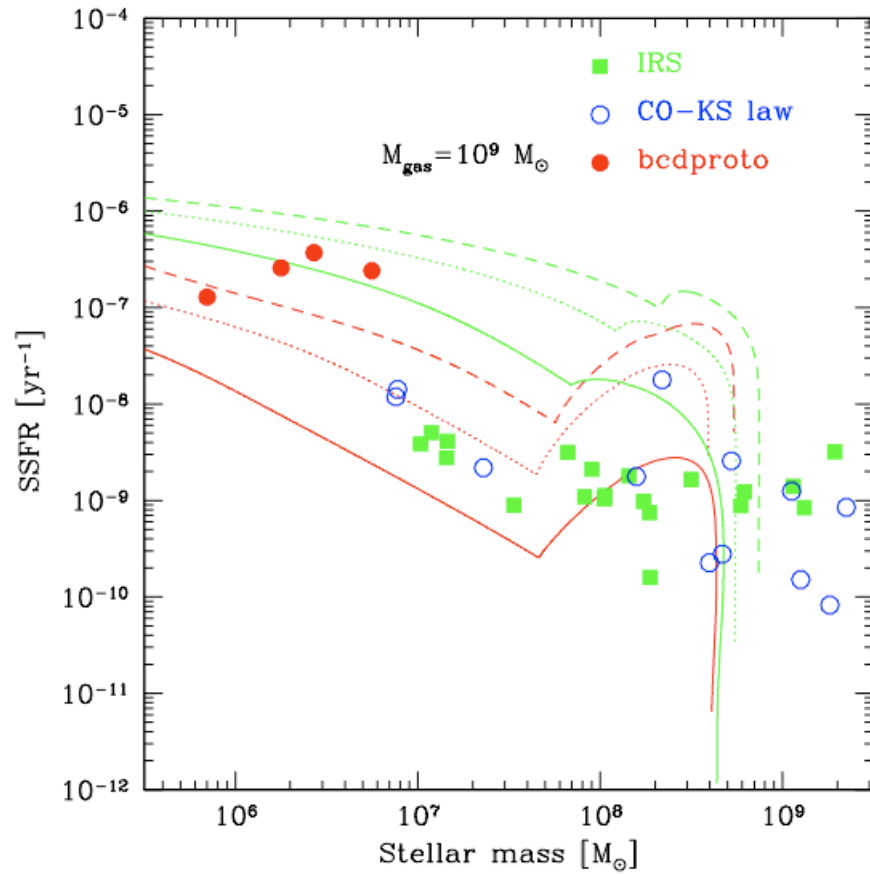


Old Model

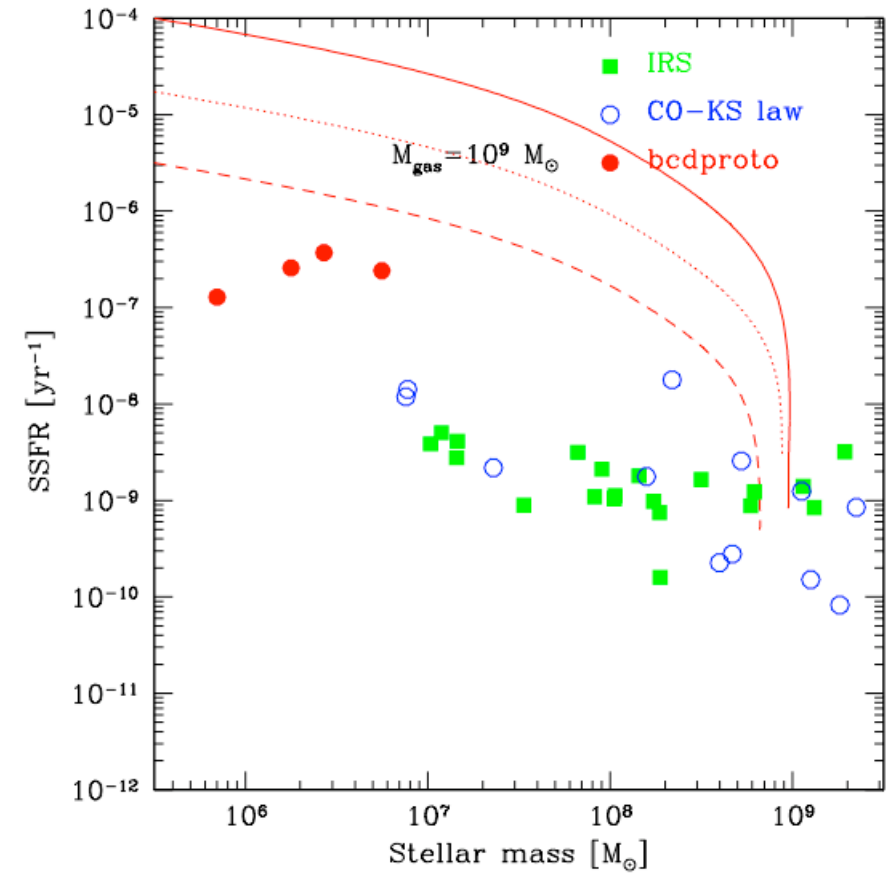


Specific star formation rate

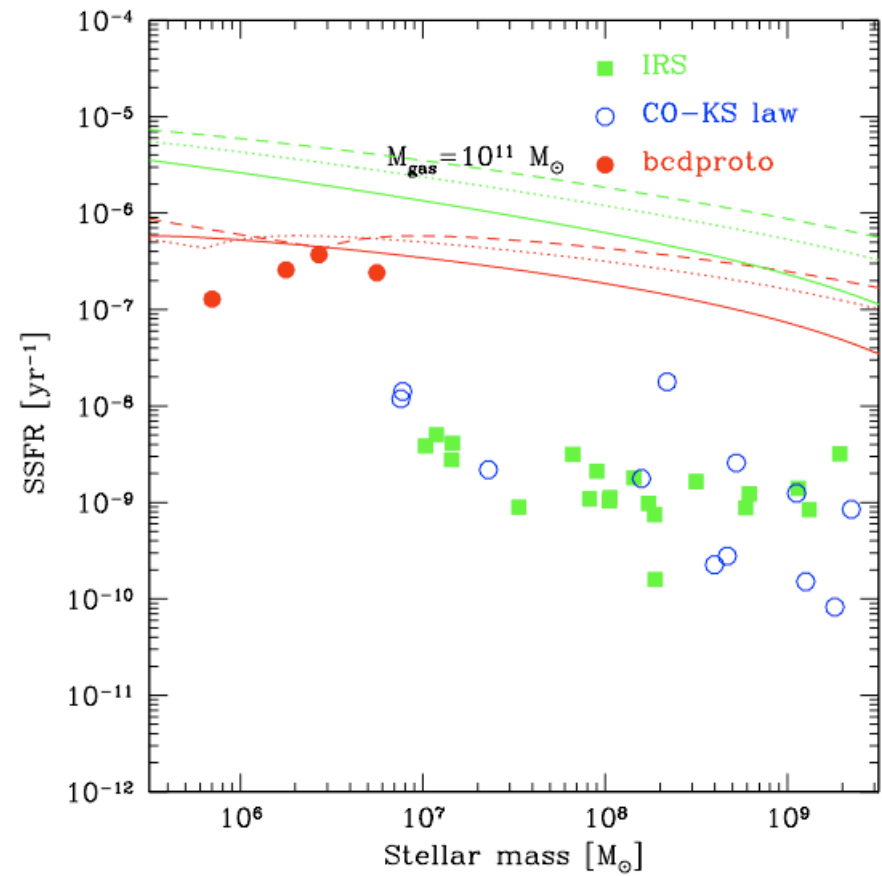
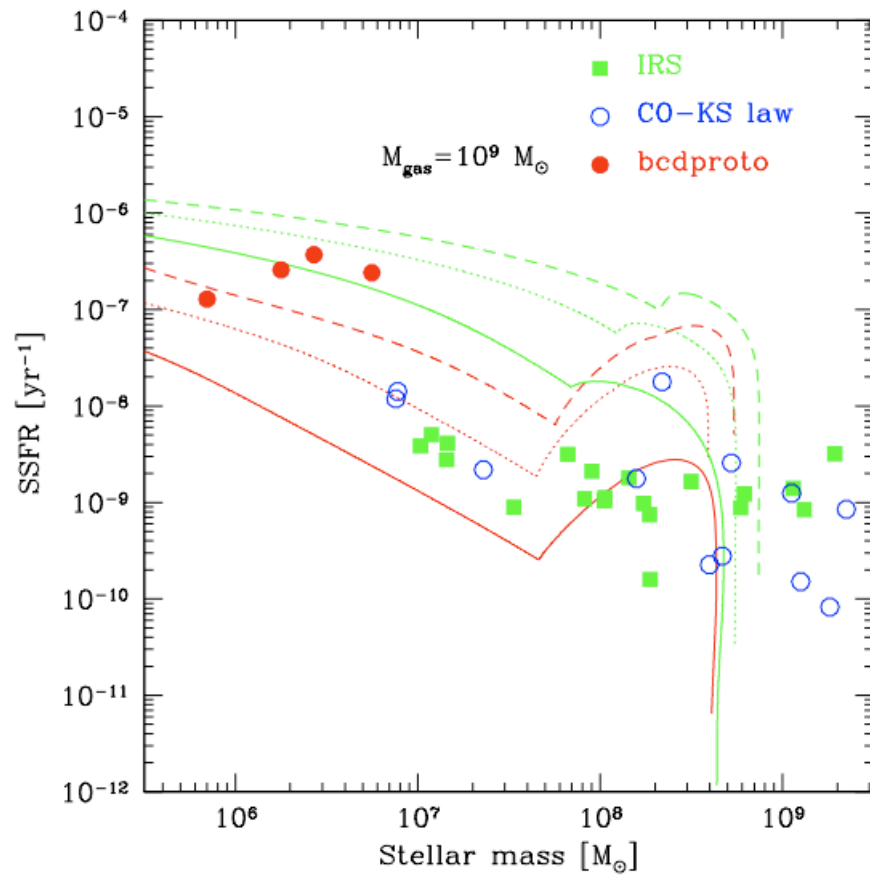
New Model



Old Model

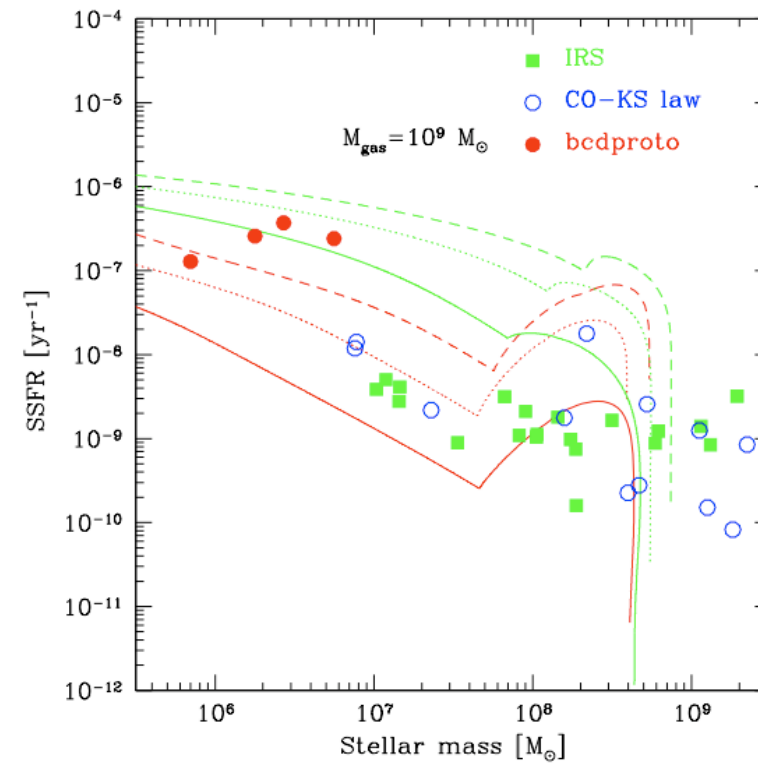
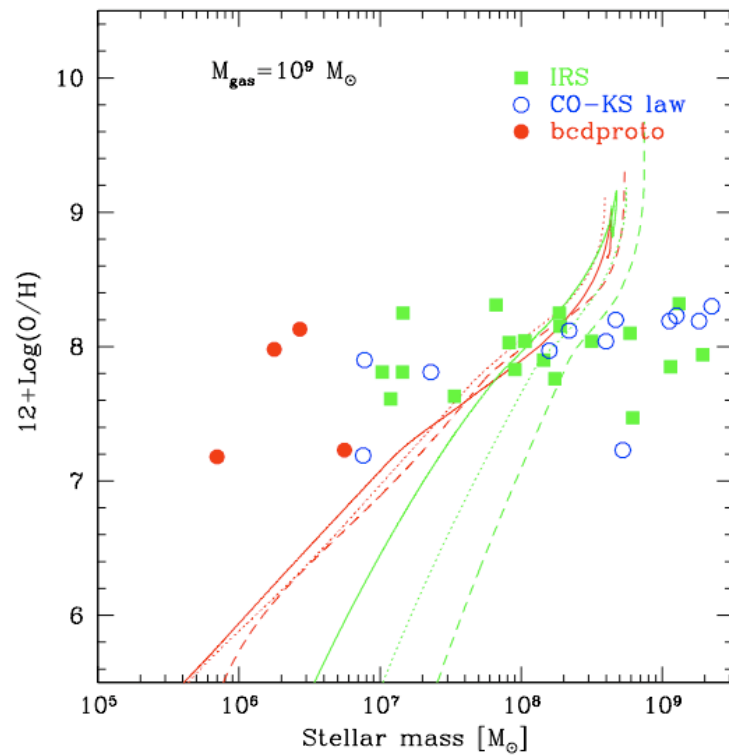


Specific star formation rate



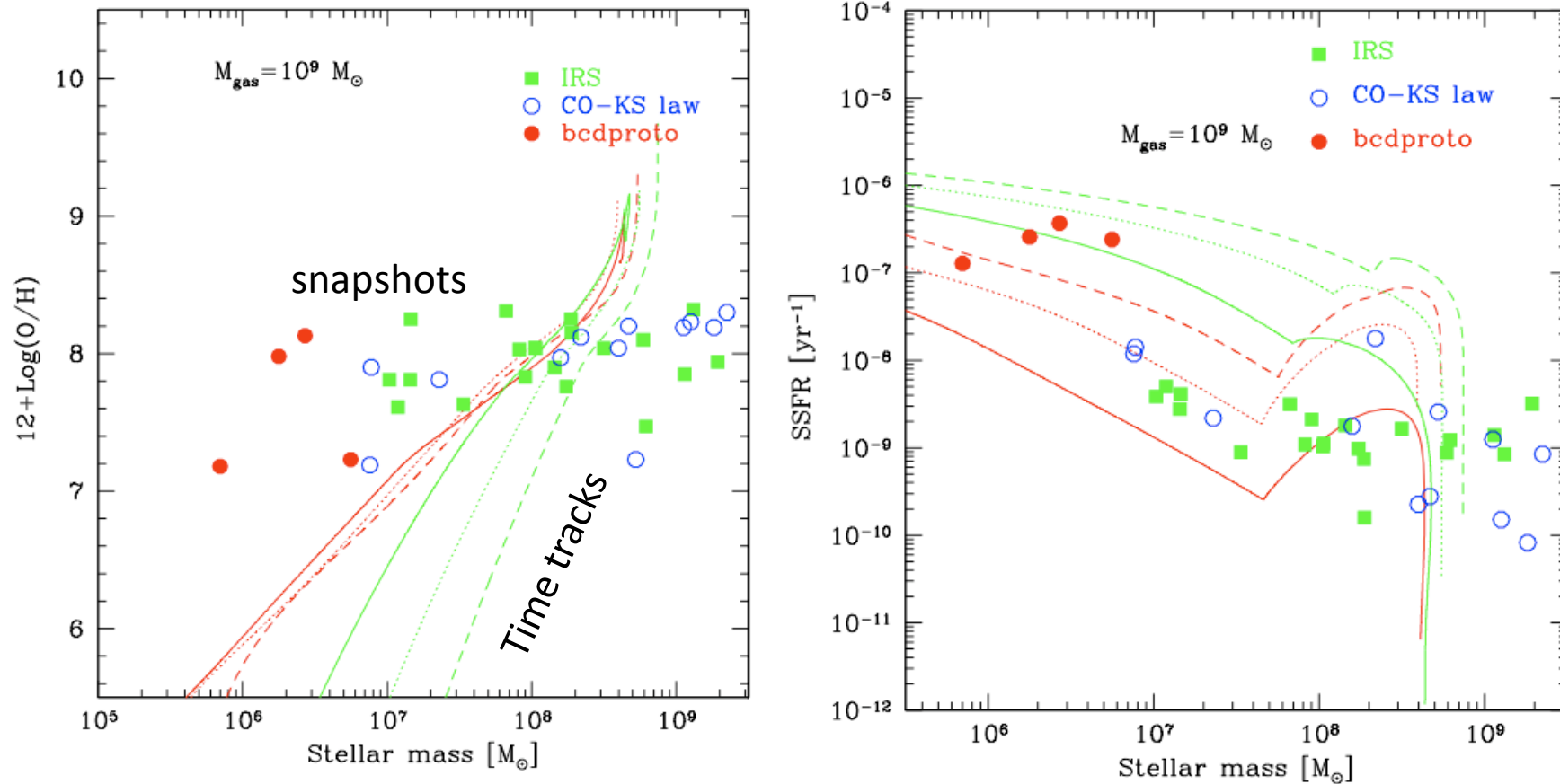
conclusions

- chemical evolution model is ok
- still need to work on the SFR prescription: are we computing f_{H_2} in the right way?
- are we comparing the models and data in the right way?



Notes for brain-storming

are we comparing the models and data in the right way?



snapshots = galaxies selected on the basis of specific properties (ex. SFRs)

→ Run a grid of models ($M_{\text{gas,in}}$, n_{HI} , n_{H_2}) and select them in terms of SFRs to populate the plane

To do list

(1) Rileggere bene il paper originale di McKee per capire bene se stiamo considerando la Sigma giusta

(2) Capire cosa conviene fare: evolvere il gas a volume density costante o a raggio costante? Cambia la dipendenza dal tempo della Sigma. Infatti:

$\Sigma \approx M_{\text{gas}}(t)^{1/3}$ se $nH = \text{cost}$

$\Sigma = M_{\text{gas}}(t)$ se $RH = \text{cost}$

(3) Intensificare la griglia di modelli per Sigma (eventualmente nH)

(4) Considerare un infall di gas alla metallicita' $Z_{\text{min}} = 5 \times 10^{-2} Z_{\text{sun}}$ e provare ad abbassare la soglia

(5) Selezionare i dati (rivisti da Leslie per essere sicuri che ci sia consistenza) in funzione della SFR, t_h e fare la stessa cosa per i dati teorici

(6) Cercare di capire le correlazioni osservate (mass-metallicity), (ssfr vs m_{star}) per poi "calibrare" la Schmidt-Kennicutt law ($\alpha_{\text{CO}}/X\text{-factor}$)