The Search for Units: A Gradient Distribution route to Multifractality in Solar Magnetic Fields

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Maybe SOC?

O Scale free, maybe SOC
O Fractals, maybe SOC
O Units, in SOC



The Why and The How

$$\nabla \cdot \mathbf{B} = \frac{\partial B}{\partial t} = R_m = \nabla \times \vec{B} = 0$$

 $\nabla \cdot \mathbf{B} = 0$ $\frac{\partial B}{\partial t} = \nabla \times (v \times B) + \eta \nabla^2 B,$ $R_m = \frac{\nabla \times (v \times B)}{\eta \nabla^2 B},$ $\vec{\nabla} \times \vec{B} = \mu_0 J$

Connection to SOC

- O allows for energy build up over timescales much longer than energy release
- O allows for a system to approach SOC
- O requires a threshold in 'energy' which must be followed by a release of energy
- O dictates energy output sizescales much less than spatial scale of system. 5

$$\nabla \cdot \mathbf{B} = \mathbf{0}$$

$$\frac{\partial B}{\partial t} = \nabla \times (v \times B) + \eta \nabla^2 B,$$

$$R_m = \frac{\nabla \times (v \times B)}{\eta \nabla^2 B},$$

$$\vec{\nabla} \times \vec{B} = \mu_0 J$$



Scale free, maybe SOC?



Abramenko 2002, 2005, 2006 Hewett, McAeer et al., 2008



Scale free, maybe SOC





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Scale free, maybe SOC



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Scale free, maybe SOC





McAteer et al., 2005

| Study | Data ^a | Method | FD ^b | |
|-----------------------------|---------------------------|--------------|--------------------------|--|
| Roudier & Muller (1987) | WL granules | DPA | 1.25 for d < 1".37 | |
| Hirzberger et al. (1997) | WL granules | D_{PA} | 1.30 for $d < 1.39$ | |
| | WL granular cells | D_{PA} | 1.16 | |
| Bovelet & Wiehr (2001) | Wl granules | D_{PA} | 1.09 | |
| Janssen et al. (2003) | B small scale | D_{PA} | $1.41 \pm 0.05, d < 1.8$ | |
| | S magnetoconvection | D_{PA} | $1.38 \pm 0.07, d < 1.8$ | |
| Tarbell et al. (1990) | B plage | D_{LA} | 1.45-1.60 | |
| Lawrence (1991) | B active region | D_{LA} | 1.56 ± 0.08 | |
| Schrijver et al. (1992) | S percolation theory | D_{LA} | 1.56 | |
| Lawrence & Schrijver (1993) | B active region | D_{LA} | 1.56 ± 0.08 | |
| Balke et al. (1993) | B plage | D_{LA} | $1.54 \pm 0.05, l < 3''$ | |
| Meunier (1999) | B active regions | D_{PA} | 1.48-1.68 | |
| | | D_{LA} | 1.78-1.94 | |
| Meunier (2004) | B active regions | D_{PA} | 1.35-1.70 | |
| Gallagher et al. (1998) | EUV quiet-Sun | DBC | 1.30-1.70 | |
| Georgoulis et al. (2002) | H α Ellerman bombs | DBC | 1.4 | |
| Fragos et al. (2004) | S cell automation | $D_{\rm BC}$ | 1.5 ± 0.1 | |
| Vlahos et al. (2002) | S cell automation | $D_{\rm BC}$ | 1.42 ± 0.12 | |
| Lawrence et al. (1993) | В | DBC | Multifractal | |
| Cadavid et al. (1994) | в | DBC | Multifractal | |
| Lawrence et al. (1996) | В | DBC | Multifractal | |

TABLE 1 FRACTAL DIMENSION ANALYSES OF SOLAR DATA

^a WL: White light; B: magnetic field; S: simulation; EUV: extreme ultraviolet.

b d: Diameter; l: length.



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McAteer et al., 2005

Corrected NOAA AR 10030, Byð



Threshold 50G

Contoured



3





McAteer et al., 2005 2700 days

9300 images



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Units, in SOC

"Where is the physics?" "Give me some units!" "The Sun is not a vacuum."

Strong gradients in the photosphere produce currents in the corona. Flares occur in the corona where currents build up.



gradients, gradients, gradients,...

1x10

1x10

1x10

1x10

1x10-6

Aaximum X-Ray Flux (Wm⁻²)





Sammis et al, ApJ, 2000, 540, 587 Schrijver, ApJ, 2007, 655, L117 Falconer et al., ApJ, 2008, 689, 1433 Al-Ghraibai, Boucheron, McAteer, ApJ, 2013



gradients, gradients, gradients





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Size of gradient at each scale or

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0 0.5 1.0

h

19

Sept, 201

D(h)

Wavelet Transform Modulus Maxima

(1) Take a *multiscale* gradient
(2) At the smallest spatial,
detect a strong gradient.
(3) Track this gradient up
through each size scale.
(4) Calculate partition function

 $\begin{aligned} \mathbf{T}_{\psi}[f](\mathbf{b}, a) \\ &= \begin{pmatrix} T_{\psi_1}[f] = a^{-2} \int d^2 \mathbf{x} \ \psi_1(a^{-1}(\mathbf{x} - \mathbf{b})) f(\mathbf{x}) \\ T_{\psi_2}[f] = a^{-2} \int d^2 \mathbf{x} \ \psi_2(a^{-1}(\mathbf{x} - \mathbf{b})) f(\mathbf{x}) \end{pmatrix}, \\ &= \nabla \{T_{\phi}[f](\mathbf{b}, a)\} \\ &= \nabla \{\phi_{\mathbf{b},a} * f\}, \end{aligned}$ (1)

$$\mathcal{M}_{\psi}[f][\mathcal{L}_{\mathbf{x}_0}(a)] \sim a^{h(\mathbf{x}_0)},$$

$$\mathcal{Z}(q,a) = \sum_{\mathcal{L} \in \mathcal{L}(a)} [\mathcal{M}_{\psi}[f](\mathbf{x} \in \mathcal{L}, a)]^{q},$$

$$h(q, a) = \sum_{\mathcal{L} \in \mathcal{L}(a)} \ln |\mathcal{M}_{\psi}[f](\mathbf{x}, a)| W_{\psi}[f](q, \mathcal{L}, a)$$
$$\sim a^{h(q)}, \tag{5}$$

$$D(q, a) = \sum_{\mathcal{L} \in \mathcal{L}(a)} W_{\psi}[f](q, \mathcal{L}, a) \ln(W_{\psi}[f](q, \mathcal{L}, a))$$

 $\sim a^{D(q)},$ (6)

The quiet Sun

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Wavelet Transform Modulus Maxima





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New flux arises near to 'strong' gradients New gradients arise near 'strong' gradients

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Problems

O We're measuring the wrong part of the active region?

- O Energy build up in *transverse* component of magnetic field.
- Magnetic field in *corona* is where the flare occurs.
- We only measure the **driver** of the build up of energy.

O What is the appropriate time scale?

- O Sun doesn't care what is happening on **24 hour timescale**.
- Is there a strong *solar cycle* dependence?
- Flaring is non-Poisson events are not independent.

O What is a big flare?

- O What is the total energy in an event? How is this distributed between radiation, particle, coronal mass ejection, etc..?
- O Careful not to succumb to big-flare syndrome





Conclusions
 The multifractal spectrum is a number distribution of gradient persistence to high spatial scales

- higher h, higher D, more energy build up
- pointer to further flux emergence and gradient build up
 - this may the connection to resulting flares.
- O Is there a maximum predictive timescale of each measure?

Looking forward O Detection of energy

release mechanism.

- how much energy is available?
- how much energy is released?
- how much energy is needed to maintain a stable active region?

O Predictions over appropriate timescales.

• How do we combine the maximum predictive timescale of each measure and flare size?



Accuracy depends: predict X class / fast CME (HSS 0.7) 12 hours predict C class (HSS 0.65) over 72 hours.

Bloomfield et al, ApJ, 2012 Also Poster Session 6.1



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Questions





Where are the gradients? Abramenko, 2005, ApJ Size Scaling index related

to structure function



Outline

O The promise of flare prediction
O The premise of flare prediction
O The problems of flare prediction







O "Big and Ugly'
 O Prediction requires understanding





magnetic field

Outline

O The promise of flare prediction
O The premise of flare prediction
O The problems of flare prediction



- O Big and Ugly?
- O Global properties are useful







Higgins et al, ASR, 2010

-Oct

2.3

| TABLE Parameters Used in the Dis | | AR properties generated by SMART | | |
|--------------------------------------------------|----|-------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------|--|
| | | AR Properties | Description | |
| Description | 1 | Type-Polarity | Unipolar/Multipolar | |
| Atmospheric | 2 | Type-Size | Big/Small | |
| Median of the granulation contrast | 3 | Type-Evolution | Emerging/Decaying | |
| Distribution of Mag | 4 | Area_Mmsq | Area of the region [Megameters squared]. | |
| Mome Magnetic Structure Detections 1-Jun-1999 | | Bflux_Mx | Total Unsigned Magnetic Flux of the region [Maxwells]. $\phi_{uns,t,i} = \sum_{pix} \phi_{t,i} $ | |
| Absol Mome Mome Mome Mome | 6 | Bfluxp_Mx | Total Positive Flux in the region [Maxwells]. $\varphi_{+,t,i} = \sum_{pix} (\varphi_{t,i} > 0)$ | |
| | 7 | Bfluxn_Mx | Total Negative Flux in the region [Maxwells]. $\phi_{-,t,i} = \sum_{pix} (\phi_{t,i} < 0)$ | |
| | 8 | Bfluximb | Flux Imbalance Fraction in the region [Fraction]. $\phi_{imb,t,i} = \frac{ (\phi_{+,t,i} - \phi_{-,t,i}) }{\phi_{uns,t,i}}$ | |
| | 9 | DBfluxDt_Mx | Flux Emergence Rate [Mx/second]. $\frac{d\phi}{dt} _{t,t} = \frac{(B_t - B_{t-\Delta t}) \times A_{cos,t,t}}{\Delta t}$ | |
| | 10 | Bmin_G | Minimum B value in the region[Gauss]. | |
| | 11 | Bmax_G | Maximum B value in the region [Gauss]. | |
| Mome Mome Total Absol | | Bmean_G | Mean B value in the region [Gauss]. | |
| | | Lnl_Mm | Neutral Line Length in the region [Mega meters]. | |
| | | Lsg_Mm | High Gradient Neutral Line Length in the region [Mega meters]. | |
| | | MxGrad_GpMm | Maximum Gradient along the Neutral Line [Gauss / Megameter]. | |
| | | MeanGrad | Mean Gradient along the Neutral Line [Gauss / Megameter]. | |
| Sum o | 17 | MednGrad | Median Gradient along the Neutral Line[Gauss / Megameter]. | |
| Total | | Rval_Mx | Schrijver R-Value[Maxwells], (Schrijver, 2007). | |
| | | WLsg_GpMm | Falconer WLsg value[Gauss / Megameter], (Falconer et al., 2008). | |
| | | R_Str | Schrijver R-Value with a lower threshold for summing flux[Maxwells]. | |
| -500 0 500 100 Momen Paul Higgins 2009 | 21 | WLsg_Str | A modified version of WLsg. | |
| Best-fit force-free twist parameter ^b | D | $a = \alpha_{\rm ff} \mathbf{v} \wedge \mathbf{p} 39$ | | |



Outline

O The promise of flare prediction
O The premise of flare prediction
O The problems of flare prediction



Conclusions

O Progress is significant

- O solar cycle of synoptic data
- O Combination of local and global properties works at HSS score of 0.8
- O Looking forward to full disk vector data.



